

# Calculus I

## Exam 1 - Review

The first exam will cover chapters 2 and 3 of Stewart's text, *Single Variable Calculus, 6e*. Exam date is Tuesday, March 10th. The exam will include many computational problems and a proof or two. I may also explicitly ask for a definition or theorem statement, though True-False type questions might also occur. The chapter reviews provide a good source of problems for practice and consideration. As you prepare for the exam, please remember the writing expectations that I have set forth. Class-time on March 9th is devoted to your questions.

### Definitions and facts to know

- Limit - "loose" definition and precise definition
- Right-hand limit and left-hand limit
- infinite limit
- continuous at a number  $a$
- discontinuous
- removable, infinite and jump discontinuity
- tangent line
- derivative of a function  $f$  (at a number  $a$ )
- differentiable at  $a$
- $\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$

### Theorems to know

- The Squeeze Theorem
- The Intermediate Value Theorem
- Theorem 8 of Section 2.5

### Computational problems

- Be able to find the derivative of a function using any one of the following rules: sum, difference, constant multiple, product, quotient, chain.
- Know the derivative of  $\sin x$  and  $\cos x$  and be able to find the derivatives of the other four trigonometric functions using some rule of differentiation.
- Be able to find a derivative using implicit differentiation.
- Solve problems from the social and natural sciences using the notion of the derivative as in Section 3.7.
- Solve related rates problems.
- Find the linearization of a function at a point  $a$ .

### Proofs

- $\epsilon - \delta$  proof for computing a limit
- Be able to prove each part of Theorem 4 of Section 2.5.
- Be able to prove Theorem 5 of Section 2.5.
- Theorem 4 of Section 3.2.
- Find the derivative of a polynomial using the limit definition of the derivative.