From: Colin Camerer Behaver of Same Theory 2003

4), patent race games (patents, Chapter 5), learning (e-commerce, Chaprium (tennis, Chapter 3), Tunisian bazaar bargaining (rug seller, Chapter startup signals guts or stupidity); a man framing a memento from when quitting after the first year of their two-year program to join a dot-com workers hustling to get a plane away from the gate on time; MBAs decidday's whale hunt, and how to divide the whale if they catch one; airline cisco commuters deciding which route to work will be quickest when the Bay when a downtrodden urban neighborhood will spring back to life; San Frantures to add to its website by trial and error; real estate developers guessing to work when the boss is away; an Arab rug seller deciding how quickly to counted price on pastries just before it closes; employees deciding how hard ter 6), stag hunt games (whalers, Chapter 7), weak-link games (airlines, knacks on eBay. These examples illustrate, respectively, ultimatum games ing what their degree will signal to prospective employers (and whether Bridge is closed; Lamelara men in Indonesia deciding whether to join the race to reach patent; an e-commerce auction company learning which fea lower his price when haggling with a tourist; rival drug firms investing in a to the left or right side of the court; the only bakery in town offering a dis interact. Here are some examples: Tennis players deciding whether to serve GAME THEORY IS ABOUT WHAT HAPPENS when people—or genes, or nations nappily married now!); and people bidding for art or oil leases, or for knickhe first met his wife, as a gift on their first official date a year later (they're (bakery, Chapter 2), gift exchange (employees, Chapter 2), mixed equilib-

and romance, Chapter 8), auctions (bidding, Chapter 9).

Chapter 7), order-statistic games (developers, Chapter 7), signaling (MBAs

I Introduction

In all of these situations, a person (or firm) must anticipate what others will do and what others will infer from the person's own actions. A game is a mathematical x-ray of the crucial features of these situations. A game consists of the "strategies" each of several "players" have, with precise rules for the order in which players choose strategies, the information they have when they choose, and how they rate the desirability (or "utility") of resulting outcomes. An appendix to this chapter describes the basic mathematics of game theory and gives some references for further reading.

Game theory has a very clear paternity. Many of its main features were introduced by von Neumann and Morgenstern in 1944 (following earlier work in the 1920s by von Neumann, Borel, and Zermelo). A few years later, John Nash proposed a "solution" to the problem of how rational players would play, now called Nash equilibrium. Nash's idea, based on the idea of equilibrium in a physical system, was that players would adjust their strategies until no player could benefit from changing. All players are then choosing strategies that are best (utility-maximizing) responses to all the other players' strategies. Important steps in the 1960s were the realization that behavior in repeated sequences of one-shot games could differ substantially from behavior in one-shot games, and theories in which a player can have private information about her values (or "type"), provided all players know the probabilities of what those types might be. In 1994, Nash, John Harsanyi, and Reinhard Selten (an active experimenter) shared the Nobel Prize in Economic Science for their pathbreaking contributions.

In the past fifty years, game theory has gradually become a standard language in economics and is increasingly used in other social sciences (and in biology). In economics, game theory is used to analyze behavior of firms that worry about what their competitors will do. Game theory is also good for understanding how workers behave in firms (such as the reaction of CEOs or salespeople to incentive contracts), the spread of social conventions such as language and fashion, and which genes or cultural practices will spread.

The power of game theory is its generality and mathematical precision. The same basic ideas are used to analyze *all* the games—tennis, bargaining for rugs, romance, whale-hunting—described in the first paragraph of this chapter. Game theory is also boldly precise. Suppose an Arab rug seller can always buy more rugs cheaply, an interested tourist values the rugs at somewhere between \$10 and \$1000, and the seller has a good idea of how

impatient the tourist is but isn't sure how much the tourist likes a particular rug. Then game theory tells you exactly what price the seller should start out at, and exactly how quickly he should cut the price as the tourist hems and haws. In experimental re-creations of this kind of rug-selling, the theory is half-right and half-wrong: it's wrong about the opening prices sellers state, but the rate at which experimental sellers drop their prices over time is amazingly close to the rate that game theory predicts (see Chapter 4).

about what players actually do. It expands analytical theory by adding emoscribing hundreds of experiments in which people interact strategically. The games. This book aims to correct the imbalance of theory and facts by deand guesses rather than careful observation of how people actually play in ematical derivation of what players with different cognitive capabilities are economics, an approach to economics which uses psychological regularity sophical perspective). Behavioral game theory is one branch of behavioral learning to analytical game theory (Colman, in press, gives a more philotion, mistakes, limited foresight, doubts about how smart others are, and results are used to create behavioral game theory. Behavioral game theory is limited its spread outside economics) and is usually based on introspection likely to do in games.² Game theory is often highly mathematical (which has periodic table of elements in chemistry. Analytical game theory is a mathonomy of strategic situations, a rough equivalent for social science of the Camerer and Loewenstein, 2003). to suggest ways to weaken rationality assumptions and extend theory (see It is important to distinguish games from game theory. Games are a tax-

Because the language of game theory is both rich and crisp, it could unify many parts of social science. For example, trust is studied by social psychologists, sociologists, philosophers, economists interested in economic development, and others. But what is trust? This slippery concept can be precisely defined in a game: Would you lend money to somebody who doesn't have to pay you back, but might feel morally obliged to do so? If you would, you trust her. If she pays you back, she is trustworthy. This definition gives a way to measure trust, and has been used in experiments in many places (including Bulgaria, South Africa, and Kenya; see Chapter 3).

The spread of game theory outside of economics has suffered, I believe, from the misconception that you need to know a lot of fancy math to apply it, and from the fact that most predictions of analytical game theory are not well grounded in observation. The need for empirical regularity to inform

^{&#}x27;Game theory fills the conceptual gap between a single monopoly, which need not worry about what other firms and consumers will do because it has monopoly power, and 'perfect competition," in which no firm is big enough for competitors to worry about. Game theory is used to study the internediate case, "oligopoly," in which there are few enough firms that each company should anticipate what the others will do.

²To be precise, this book is only about "noncooperative" game theory—that is, when players cannot make binding agreements about what to do, so they must guess what others will do. Cooperative game theory is a complementary branch of game theory which deals with how players divide the spoils after they have made binding agreements.

1.1 What Is Game Theory Good For?

seminal book, von Neumann and Morgenstern (1944, p. 4) wrote: game theory has been recognized many times. In the opening pages of their

is no reason to hope for an easier development in economics. zation of that subject was achieved. . . . It would have been absurd in smaller than that commanded in physics at the time when mathemati-Our knowledge of the relevant facts of economics is incomparably physics to expect Kepler and Newton without Tycho Brahe—and there the empirical background of economic science is definitely inadequate

what they know, the order in which they move, and so forth. As Crawford depend sensitively on the choices players have, how they value outcomes, mental control is particularly useful because game theory predictions often (1997, p. 207) explains: (particularly in clearly structured situations such as auctions). But experitheory has also been tested using data that naturally occur in field settings This book is focused on experiments as empirical background. Game

ronment. . . . For many questions, [experimental data are] the most advantage in identifying the relationship between behavior and envivariables. Important advances in experimental technique over the past often compounded in the field by an inability to observe all relevant so that strategic models carry a heavy informational burden, which is likely to be less reliable than casual empiricism or introspection. important source of empirical information we have, and [they are] unthree decades allow a control that often gives experiments a decisive Behavior in games is notoriously sensitive to details of the environment,

of players, complex environments, communication, and overlapping generations' would enhance generalizability further, and people should do more money, which are usually small. But more ambitious experiments with teams mensions of generalizability—particularly the effects of playing for more of the experimental method per se. Experimenters have studied a few dieralizability are a demand for more elaborate experiments, not a dismissal strategy, diplomats negotiating, and so forth. But these doubts about gennancial stakes generalize to workers in firms, companies creating corporate with (mostly) college students playing for a couple of hours for modest fi-Of course, it is important to ask how well the results of experiments

1.1 What Is Game Theory Good For?

more than finding that cashiers sometimes give the wrong change disproves way theory says, their behavior has not proved the mathematics wrong, any players with various degrees of rationality will do. If people don't play the simply "analytical," a body of answers to mathematical questions about what what? The theorist's answer is that game theory is none of the above—it is Is game theory meant to predict what people do, to give them advice, or

rational bidders will pay. such as an oil lease or a painting, auction theory then derives how much about the rules of the auction and the way in which bidders value an object, good example of all three uses of game theory. Based on precise assumptions predict, and also to explain (or "postdict"4) and prescribe. Auctions are a In practice, however, the tools of analytical game theory are used to

artificial bid to force the high bidder to pay more). auctions are vulnerable to manipulation by the seller (who can sneak in an bidder pays a price other than what she bid in a second-price auction, such Reilly, 2000). Why? Game theory offers an explanation: Since the high bidder pays what she bid. But second price auctions are rare (see Lucking than others. For example, in "second-price" or Vickrey auctions the high revenue for sellers than traditional first-price auctions in which the high bid. Under some conditions these auctions should, in theory, raise more bidder buys the object being auctioned at a price equal to the second-highest Theory can help explain why some types of auction are more common

mapping values into bids is nonlinear and counterintuitive.⁵ ably close to the amounts they are predicted to, even when the function the object (and doesn't care how much others value it), people bid remark Kagel and Levin, in press). The results of these experiments are mixed. In lematic: Because bidders' valuations are usually hidden, it is difficult to private-value auctions in which each player has her own personal value for tested. Fortunately, there are many careful experiments (see Kagel, 1995; tell whether they are bidding optimally, although some predictions can be How well does auction theory predict? Tests with field data are prob-

example—different oil companies would all value the oil in the same way optimistic about the value of the object tend to bid the highest and win but aren't sure how much oil is there. In these auctions players who are most same for everyone, but is uncertain. Bidding for leases on oil tracts is an In common-value auctions the value of the object is essentially the

³ See Schotter and Sopher (2000).

event unfolded are called "analytical narratives" and are proving increasingly popular (Bates et al., 1998). 4 In some domains of social science, these kinds of game-theoretic "stories" about how an institution or

⁵See Chen and Plott (1998) and the scaled-bid mechanism results in Chapter 4.

The problem is that, if you win, it means you were much more optimistic than any other bidder and probably paid more than the object is worth, a possibility called the "winner's curse." Analytical game theory assumes rational bidders will anticipate the winner's curse and bid very conservatively to avoid it. Experiments show that players do not anticipate the winner's curse, so winning bidders generally pay more than they should.

tion raises government revenue and, ideally, ensures that a public resource ends up in the hands of the firms that are best able to create value from and regulators, and using the results of testbedding to improve designs. Aucmotivated bidders could exploit loopholes in designs proposed by lawyers on auction theory. Instead, theorists spent a lot of time pointing out how which float). The designs that emerged were not exactly copied from books of an airplane wing, or a "tow-tank" pool to see which ship designs sink and weaknesses in proposed designs (like using a wind tunnel to test the design guessing accurately how players will actually behave—good prediction—is mutual rationality. Notice that, in this process of design and prescription, closer to the ideas in this book than to standard theory based on unlimited choices reflect an implicit theory of actual behavior in games that is probably designers were not willing to bet that behavior would actually be equivalent "Vickrey" auction, in which the highest bidder pays what the second-highest slowly until only one bidder remains, is revenue-equivalent to a sealed-bid structure. (For example, an "English" auction, in which prices are raised ones. One of the most powerful and surprising ideas in auction theorymunications Commission opens the envelopes and announces the highest bid" design in which bidders simply mail in bids and the Federal Comtion designers opted for a design that gave bidders a chance to learn from theorists and experimental "testbedding" that helped detect unanticipated it. In most countries, the auctions were designed in collaborations among scribe how to bid in an auction, or how to design an auction. The shinin different types of auctions, despite what theory predicted. Their design nies would participate in with billions of dollars on the line, the auction bidder bid.) But when it came to designing an auction that actual compathe same amount of revenue as other auctions that are quite different in "revenue equivalence"—is that some types of auctions will, in theory, raise potential mistakes and from watching others, rather than a simpler "sealedregulatory agencies decided to put airwave spectrum up for auction. An aucing triumphs of modern auction theory are recent auctions of airwaves to telecommunications companies. In several auctions in different countries, Perhaps the most important modern use of auction theory is to pre-

1.2 Three Examples

Even if game theory is not always accurate, descriptive failure is prescriptive opportunity. Just as evangelists preach because people routinely violate moral codes, the fact that players violate game theory provides a chance to give helpful advice. Simply mapping social situations into types of games is extremely useful because it tells people what to look out for. In their popular book for business managers, Co-opetition, Brandenburger and Nalebuff (1996) draw attention to the barest bones of a game—players, information, actions, and outcomes. Both are brilliant theorists who could have written a more theoretical book. They chose not to because teaching MBAs and working with managers convinced them that teaching the basic elements of game theory is more helpful.

Game theory is often used to prescribe in a subtler way. Sometimes game theory is used to figure out what it is likely to happen in a strategic interaction, so a person or company can then try to change the game to their advantage. (This is a kind of engineering approach too, since it asks how to improve an existing situation.)

1.2 Three Examples

This chapter illustrates the basics of behavioral game theory and the experimental approach with three examples (which are discussed in more detail in later chapters): ultimatum bargaining, "continental divide" coordination games, and "beauty contest" guessing games. Experiments using these games show how behavioral game theory can explain what people do more accurately by extending analytical game theory to include how players feel about the payoffs other players receive, limited strategic thinking, and learning.

The three games use a recipe underlying most of the experiments reported in this book: pick a game for which standard game theory makes a bold prediction or a vague prediction that can be sharpened. Simple games are particularly useful because only one or two basic principles are needed to make a prediction. If the prediction is wrong, we know which principles are at fault, and the results usually suggest an alternative principle that predicts better.

In the experiments, games are usually posed in abstract terms because game theory rarely specifies how adding realistic details will affect behavior. Subjects make a simple choice, and know how their choices and the choices of other subjects combine to determine monetary payoffs. Subjects are

⁶ Howard Raiffa pointed this out many times, calling game theory "asymmetrically normative."

⁷These design choices bet heavily on the cognitive presumption that people are using generic principles of surategic thinking which transcend idiosynetatic differences in verbal descriptions of games. If choices are domain specific then the basic enterprise this book describes is incomplete; varying game labels to evoke

1.2 Three Example:

actually rewarded based on their performance because we are interested in extrapolating the results to naturally occurring games in which players have substantial financial incentives. The games are usually repeated because we are interested in equilibration and learning over time. An appendix to this chapter describes some key design choices experimenters make, and why they matter.

1.2.1 Example 1: Ultimatum Bargaining

I once took a cruise with some friends and a photographer took our picture, unsolicited, as we boarded the boat. When we disembarked hours later, the photographer tried to sell us the picture for \$5 and refused to negotiate. (His refusal was credible because several other groups stood around deciding whether to buy their pictures, also for \$5. If he caved in and cut the price, it would be evident to all others and he would lose a lot more than the discount to us since he would have to offer the discount to everyone.) Being good game theorists, we balked at the price and pointed out that the picture was worthless to him (one cheapskate offered \$1). He rejected our insulting offer and refused to back down.

The game we played with the photographer was an "ultimatum game," which is the simplest kind of bargaining. In an ultimatum game there is some gain from exchange and one player makes a take-it-or-leave-it offer of how to divide that gain. Our picture presumably had no value to him and was valuable to us (worth more than \$5 in sentimental value). A price is simply proposing a way to divide the gains from exchange between our true reservation price and his cost. His offer to sell for \$5 was an ultimatum offer because he refused to negotiate.

In laboratory ultimatum games like this, two players, a Proposer and a Responder, bargain over some amount, say \$10 (the sum used in many experiments). The \$10 represents the value of the gain to exchange (or "surplus") that would be lost if the trade wasn't made. The Proposer offers x to the Responder, leaving herself \$10 - x. The Responder can either take the offer—then the Responder gets x and the Proposer gets \$10 - x—or reject it and both get nothing.

Because the ultimatum game is so simple, it is not a good model of the protracted process of most naturally occurring bargaining (and isn't intended to be). It is the right model of what happened to us after the cruise,

domain-specific reasoning is the next step. The study by Cooper et al. (1999) of ratchet effects in productivity games using Chinese factory managers—who face such effects in planned economics—is a good example (see Chapter 8).

and what happens in the waning minutes before a labor strike is called, or on the courthouse steps before a lawsuit goes to trial. It is a model of the last step in much bargaining, and hence is a building block for modeling more complicated situations (see Chapter 4).

Simple games test game-theoretic principles in the clearest possible way. Ultimatum games, and related games, also are useful for measuring how people feel about the allocations of money between themselves and others.

The analytical game theory approach to ultimatum bargaining is this: First assume players are "self-interested"; that is, they care about earning the most money for themselves. If players are self-interested, the Responder will accept the smallest money amount offered, say \$0.25. If the Proposer anticipates this, and wants to get the most she can for herself, she will offer \$0.25 and keep \$9.75. In formal terms, offering \$0.25 (and accepting any positive amount) is the "subgame perfect equilibrium". By going first, the Proposer has all the bargaining power and, in theory, can exploit it because a self-interested Responder will take whatever she can get.

To many people, the lopsided distribution of the \$10 predicted by analytical game theory (with self-interest) seems unfair. Because the allocation is considered unfair, the way people actually bargain shows whether people are willing to take costly actions that express their concerns for fairness. In the cruise-picture example, offering \$1 instead of the \$5 price the photographer offered added \$4 to our surplus and subtracted \$4 from his. If he thought this was unfair to him, he could reject it and earn nothing (even though everyone suffers—he earns no money and we don't get a picture we would like to own). The lab experiments simulate this simple game. Will Responders put their money where their mouths are and reject offers that seem unfair? If so, will Proposers anticipate this and make fair offers, or stubbornly make unfair offers?

In dozens of experiments conducted in several different countries, Proposers offer \$4 or \$5 out of \$10 on average, and offers do not vary much. Offers of \$2 or less are rejected about half the time. The Responders think much less than half is unfair and are willing to reject such small offers, to punish the Proposer who behaved so unfairly. Figure 1.1 shows data from a study by Hoffman, McCabe, and Smith (1996a). The x-axis shows the amount being offered to the Responder, and the y-axis shows the relative frequency of offers of different amounts. The dark part of each frequency bar is the number of offers that were rejected. Most offers are close to half

Note also that every offer is a "Nash equilibrium" or mutual best-response pattern because x is the optimal offer if the Proposer thinks the Responder will reject any other offen (This belief may be wrong but, if the Proposer believes it, she will never take an action that disconfirms her belief, so the wrong belief can be part of a Nash equilibrium.)

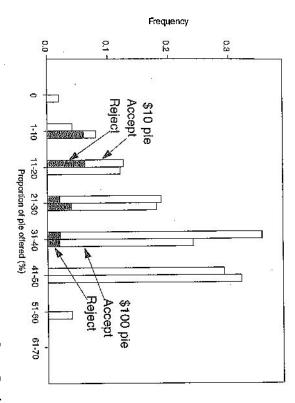


Figure 1.1. Offers and rejections in high- and low-stakes ultimatum games. Source: Based on data from Hoffman, McCabe, and Smith (1996a).

and low offers are often rejected. Figure 1.1 also shows that the same pattern of results occurs when stakes were multiplied by ten and Arizona students bargained over \$100. (A couple of subjects rejected \$30 offers!) The same basic result has been replicated with a \$400 stake (List and Cherry, 2000) in Florida and in countries with low disposable income, including Indonesia and Slovenia, where modest stakes by American standards represent several weeks' wages.

There are many interpretations of what causes Responders to reject substantial sums (see Chapter 3). There is little doubt that some players define a fair split of \$10 as close to half and have a preference for being treated fairly. Such rejections are evidence of "negative reciprocity": Responders reciprocate unfair behavior by harming the person who treated them unfairly, at a substantial cost to themselves (provided the unfair Proposer is harmed more than they are). Negative reciprocity is evident in other social domains, even when monetary stakes are high—jilted boyfriends who accost their exes, ugly divorces that cost people large sums, impulsive street crimes caused by a stranger allegedly "disrespecting" an assailant, the failure of parties in le-

gal "nuisance cases" to renegotiate after a court judgment even when both could benefit (Farnsworth, 1999), and so on.9

This explanation for ultimatum rejections begs the question of where fairness preferences came from. A popular line of argument is that human experience in our ancestral past created evolutionary adaptations in brain mechanisms, or in the interaction of cognitive and emotional systems, which cause people to get angry when they are pushed around because getting angry had survival value when people interacted with the same people in a small group (see Frank, 1988). A different line of argument is that cultures create different standards of fairness, perhaps owing to the closeness of kin relations or the degree of anonymous market exchange with strangers (compared with sharing among relatives), and these cultural standards are transmitted socially through oral traditions and socialization of children.

Remarkable evidence for the cultural standards view comes from a study by eleven anthropologists who conducted ultimatum games in primitive cultures in Africa, the Amazon, Papua New Guinea, Indonesia, and Mongolia (see Chapter 2). In some of these cultures, people did not think that sharing fairly was necessary. Proposers in these cultures offered very little (the equivalent of \$1.50 out of \$10) and Responders accepted virtually every offer. Ironically, these simple societies are the only known populations who behave exactly as game theory predicts!

Note that rejections in ultimatum games do not necessarily reject the strategic principles underlying game theory (for example, Weibull, 2000). The Responder simply decides whether she wants both players to get nothing, or wants to get a small share when the Proposer gets much more. The fact that a Responder rejects means she is not maximizing her own earnings, but it does not mean she is not capable of strategic thinking. Recent theories attempt to explain rejections using social preference functions which balance a person's desire to have more money with their desire to reciprocate those who have treated them fairly or unfairly, or to achieve equality. Such functions have a long pedigree (traceable at least to Edgeworth in the 1890s). Economists have resisted them because it seems to be too easy to introduce a new factor in the utility function for each game. But the new theories strive to explain results in different games with a single function. Having a lot of data from different games to work with makes this enterprise possible and imposes discipline.

⁹My sister Jeannine told me that in Atlantic City the casinos sometimes have problems with lucrative "high-roller" customers stealing luxurious towels, robes, and other items from their (complimentary) hotel rooms after losing at the casinos. In their minds these losers are simply taking things they have paid for

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1.2

Three Examples

The new theories make surprising new predictions. For example, when there are two or more Proposers, there is no way for any one of them single-handedly to earn more money and limit inequality. As a result some theories predict that both Proposers offer almost everything to the Responder even though they do care about equality. (If there had been two photographers on that damn boat, we would have gotten our picture for \$1.)

New social preference theories should prove useful in analyzing bargaining, tax policy, the strong tendency of tenant farmers to share crop earnings equally with landowners (Young and Burke, 2001), and wage-setting (particularly the reluctance of firms to cut wages in hard times, which is puzzling to economists who assume changes in the price of labor will equalize supply and demand, and other phenomena).

1.2.2 Example 2: Path-Dependent Coordination in "Continental Divide" Games

In coordination games, players want to conform to what others do (although they may have different ideas about which conformist convention is best). For example, in California there is an ongoing struggle over the physical location of the "new media" firms, such as internet provision of film and entertainment. New media people could gravitate toward Silicon Valley, where web gecks congregate, or toward Hollywood and Southern California.

is the better location depends on whether you think the location of internet firms is central, and "content" producers should follow them, or whether the internet is merely a distribution channel and content providers are king.¹⁰

This economic tug-of-war can be modeled by a game in which players choose a location, and their earnings depend on the location they choose and the location most other people choose. A game with this flavor has been studied by Van Huyck, Battalio, and Cook (1997). Table 1.1 shows the payoffs (in cents). In this game, players pick numbers from 1 to 14 (think of the numbers as corresponding to physical locations—low numbers are Hollywood and high numbers are Silicon Valley). The matrix in Table 1.1 shows the row player's payoff from choosing a number when the median number everyone in a group picks—the middle number—is the number in the different columns. If you choose 4, for example, and the median is 5, you earn a healthy payoff of 71; but if the median is 12 you earn 14 (bankruptcy!). The basic payoff structure implies you should pick a

¹⁰Of course, this example is undermined by the fact that cyberspace is everywhere and nowhere, so content providers might be able to stay put in the swank Hollywood Hills and still do business "in" Silicon Valley without moving.

low number if you think most others will pick low numbers, and pick a high number if you think most others will pick high numbers. If you aren't sure what others will do, pick a number such as 6, which gives payoffs ranging from 23 to 82 (hedging your bet).

In the experiments, players are organized into seven-person groups. The groups play together fifteen times. After each trial you learn what the median was, compute your earnings from that trial (depending on your own choice and the median), and play again. Since the game is complicated, think for a minute about what you would actually do and what might happen over the course of playing fifteen times.

The payoffs have the property that, if a player guesses that the median number is slightly below 7, her best response to that guess is to choose a number smaller than the guess itself. For example, if you think the median will be 7, your best response is 5, which earns 83 cents. Thus, if medians are initially low, responding to low medians will drive numbers lower until they reach 3. Three is an equilibrium or mutual best-response point because, if everyone chooses 3, the median will be 3 and your best response to a median of 3 is to choose 3. If players were to reach this point, nobody could profit by moving away. (The payoff from this equilibrium is shown in italics in Table 1.1.)

14	13	12	11	10	9	œ	7	O	Œ	4	ယ	13	-	Choice		
-217	-173	-133.	-97	8; 1	-37	-13	7	23	35	43	48	48	£	-		
-198	-156.	-117.	-82	-51	-24	_	18	33	44	51	54	53	49	N		
-179 -	-137 -	⁻ 100	-66	-87	-	11	28	42	52	от 00	60	58 80	52	ပာ		
-168 -	-118	82	-49	-21	ţ ₃	23	40	52	60	65	66	62	55	44.		
-134 -	-96	-61	-31 31	_4	18	37	51	62	69	71	70	6	56	טיז		
-105	-69	-37	-9	15	35	51	64	72	77	77	74	66	Ç,	Q	×	
-65	-33	-5	20	40	57	69	78	82	83	80	72	61	46	7	Median choice	
52	67	78	85	89	88	83	75	62	4 6	26	_	-27	-59	တ	choice	
72	83	16	94	94	89	81	69	53	32	∞	-20	-52	-88	9	"	
S.	94	99	001	98	91	80	60	47	25	10	32	-67	-105-	10		
95	103	106	105	101	92	80	64	43	19	6	-41	-77	-117	11		
104	110	I12	110	104	94	80	63	41	15	-14	-48	-86	-127	12		
112	117	816	114	107	96	81	62	39	12	-19	-53	-92	-135	139		
120	123	123	119	110	98	82	62	38	10	-22	−58	-98	-142	Ĭ4		

Source: Van Huyck, Battalio, and Cook (1997).

1.2 Three Examples

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But there is another Nash equilibrium. If players guess that the median will be 8 or above, they should choose numbers that are higher than their guesses, until they reach 12; 12 is also a Nash equilibrium because choosing 12 gives the highest payoff if the median is 12.

This is a coordination game because there are two Nash equilibria in which everybody chooses the same strategy. Game theorists have struggled for many decades to figure out which of many equilibria will result if there are more than one.

broken ones spreads throughout the community like a virus. Policymakers love the broken window theory because it suggests an easy fix single broken window can lead to a spiralling process of social breakdown. aren't watchful and other criminals are lurking (so the cops are busy), a Since criminals want to commit crimes in communities where neighbors replace their own broken windows, and put fresh paint on their houses. in a community, neighbors feel less obligation to keep their yards clean, Anecdotal evidence suggests that, when there is a single broken window Another example is what social theorists call the "broken window effect." in Bolivia. If that butterfly had just sat still, the Bolivians would be dryl set in motion a complicated meteorological process that creates a storm is a complex dynamic system, the movement of a butterfly in China can example is what chaos theorists call the "Lorenz effect": Because weather in which small historical accidents have a big long-run impact. A famous to problems of urban decay—repair every window before the effect of a few This particular game illustrates processes in nature and social systems

I call the game in Table 1.1 the "continental divide" game. The continental divide is a geographic line which divides those parts of North America in which water will flow in one direction from the parts in which water flows in the opposite direction. If you stand on the continental divide in Alaska, and pour water from a canteen as I once did, some drops will flow north to the Arctic Ocean and others will flow to the Pacific Ocean. Two drops of water that start out infinitesimally close together in the canteen end up a thousand miles apart.

The game is called the continental divide game because medians below 7 are a "basin of attraction" (in evolutionary game theory terms) for convergence toward the equilibrium at 3. Medians above 8 are a basin of attraction for convergence toward 12. The "separatrix" between 7 and 8 divides the game into regions where players will "flow" toward 3 and players will flow toward 12.

Which equilibrium is reached has important economic consequences. The 12 equilibrium pays \$1.12 for each player but the 3 equilibrium pays only \$0.60. On this basis alone, you might guess that players would choose higher numbers in the hopes of reaching the more profitable equilibrium. Before glancing ahead, ask yourself again what you think will happen. If you

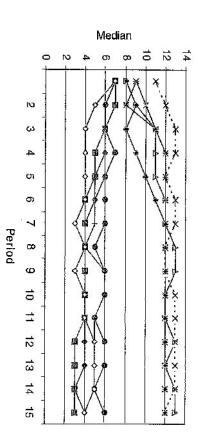


Figure 1.2. Median choices in the "continental divide" game. Source: Based on data from Van Huyck, Battalio, and Cook (1997).

have studied a lot of game theory and still aren't sure what to expect, your curiosity about what people actually do should be piqued.

Figure 1.2 shows what happened in ten experimental groups. Five groups started at a median at 7 or below, all of them flowed toward the low-payoff equilibrium at 3. The other five groups started at 8 or above and flowed to the high-payoff equilibrium.

The experiment has two important findings. First, people do not always gravitate toward the high-payoff equilibrium even though players who end up at low numbers earn half as much. (Whether they would if they could play again, or discussed the game in advance, is an interesting open question.) Second, the currents of history are strong, creating "extreme sensitivity to initial cónditions." Players who find themselves in a group with two or three others who think 7 is their lucky number, and choose it in the first period, end up sucked into a whirlpool leading to measly \$0.60 earnings. Players in a group whose median is 8 or higher end up earning almost twice as much. One or two Chinese subjects choosing 8—a lucky number for Chinese—could bring good fortune to everyone, just as the butterfly brought rain on the Bolivians.

No concept in analytical game theory gracefully accounts for the fact that some groups flow to 3 and earn less, while others flow to 12 and earn more. Indeed, the problem of predicting which of many equilibria will result in games such as these may be inherently unsolvable by pure reasoning. Social conventions, communication, subtle features of the display of the game, analogies players draw with experiences they have had, and homespun ideas about lucky numbers could all influence which equilibrium is reached. As

Schelling (1960) wrote, predicting what players will do in these games by pure theory is like trying to prove that a joke is funny without telling it.

1.2.3 Example 3: "Beauty Contests" and Iterated Dominance

In Keynes's famous book General Theory of Employment, Interest, and Money, he draws an analogy between the stock market and a newspaper contest in which people guess what faces others will guess are most beautiful: "It is not a case of choosing those which, to the best of one's judgment, are really the prettiest, nor even those which average opinion genuinely thinks the prettiest. We have reached the third degree, where we devote our intelligences to anticipating what average opinion expects the average opinion to be. And there are some, I believe, who practise the fourth, fifth, and higher degrees" (1936, p. 156). This quote is perhaps no more apt than in the year 2001 (when I first wrote this), just after prices of American internet stocks soared to unbelievable heights in the largest speculative bubble in history. (At one point, the market valuation of the e-tailer bookseller Amazon, which had never reported a profit, was worth more than all other American booksellers combined.)

A simple game that captures the reasoning Keynes had in mind is called the "beauty contest" game (see Nagel, 1995, and Ho, Camerer, and Weigelt, 1998). In a typical beauty contest game, each of N players simultaneously chooses a number x_i in the interval [0,100]. Take an average of the numbers and multiply by a multiple p < 1 (say p = 0.7). The player whose number is closest to this target (70 percent of the average) wins a fixed prize. Before proceeding, think about what number you would pick.

The beauty contest game can be used to distinguish whether people "practise the fourth, fifth, and higher degrees" of reasoning as Keynes wondered. Here's how, Most players start by thinking, "Suppose the average is 50". Then you should choose 35, to be closest to the target of 70 percent of the average and win. But if you think all players will think this way the average will be 35, so a shrewd player such as yourself (thinking one step ahead) should choose 70 percent of 35, around 25. But if you think all players think that way you should choose 70 percent of 25, or 18.

In analytical game theory, players do not stop this iterated reasoning until they reach a best-response point. But, since all players want to choose 70 percent of the average, if they all choose the same number it must be zero. (That is, if you solve the equation $x^* = 0.7x^*$, you've found the unique Nash equilibrium.)

The beauty contest game provides a rough measure of the number of steps of strategic thinking that subjects are doing. It is called a "dominance-solvable game" because it can be "solved"—i.e., an equilibrium can be

computed—by iterated application of dominance. A dominated strategy is one that yields a lower payoff than another (dominant) strategy, regardless of what other players do. Choosing a number above 70 is a dominated strategy because the highest possible value of the target number is 70, so you can always do better by choosing a number lower than 70. But if nobody violates dominance by choosing above 70, then the highest the target can be is 70 percent of 70, or 49, so choosing 49–70 is dominated if you think others obey one step of dominance. Deleting dominated strategies iteratively leads you to zero.

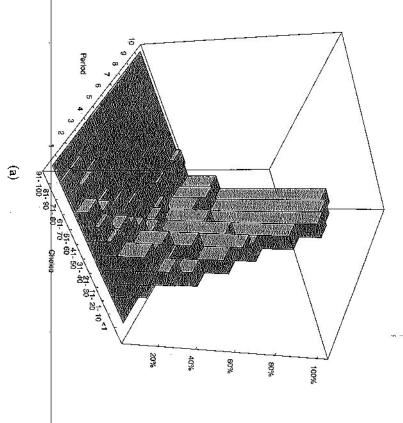
Many interesting games are dominance solvable. A familiar example in economics is Cournot duopoly. Two firms each choose quantities of similar products to make. Since their products are the same, the market price is determined by the total quantity they make (and by consumer demand). It is easy to show that there are quantities so high that firms will lose money because flooding the market with so much supply will drive prices too low to cover fixed costs. If you assume your rivals won't produce that much, then somewhat lower quantities are bad (dominated) choices for you. Applying this logic iteratively leads to a precise solution.

In practice, it is unlikely that people perform more than a couple of steps of iterated thinking because it strains the limits of working memory (i.e., the amount of information people can keep active in their mind at one time). Consider embedded sentences such as "Kevin's dog bit David's matiman whose sister's boyfilend gave the dog to him." Who's the "him" referred to at the end of the sentence? By the time you get to the end, many people have forgotten who owned the dog because working memory has only so much space. I Embedded sentences are difficult to understand. Dominance-solvable games are similar in mental complexity.

Iterated reasoning also requires you to believe that others are thinking hard, and are thinking that you are thinking hard. When I played this game at a Caltech board of trustees meeting, a very clever board member (a well-known Ph.D. in finance) chose 18.1. Later he explained his choice: He knew the Nash equilibrium was 0, but figured the average Caltech board member was clever enough to do two steps of reasoning and pick 25. Then why not pick 17.5 (which is 70 percent of 25)? He added 0.6 so he wouldn't tie with people who picked 17.5 or 18, and because he guessed that a few people would pick high numbers, which would push the average up. Now that's good behavioral game theory! (He didn't win, but was close.)

What happens in beauty contest games? Figure 1.3 shows choices in beauty contests with p=0.7 with feedback about the average given to

¹¹Seeing the sentence on the written page makes it easier; try reading it aloud to somebody who must remember the words and cannot refer back to them.



published data from Ho, Camerer, and Weigelt. Figure 1.3. Convergence in low-stakes and high-stakes "beauty contest" games. Source: Un-

subjects after each of ten rounds (unpublished data from Ho, Camerer, and results from games with low-stakes payoffs (a \$7 prize per period for seventervals (on the side) across ten rounds (in front). The first histogram shows Weigelt). Bars show the relative frequency of choices in different number in-(\$28) payoffs. person groups) and the second histogram shows results from high-stakes

choosing zero is being too smart for your own good! zero. The goal is to be one step ahead of the average but no further and the equilibrium of zero in the first round. In fact, they should not choose cated that the median subject uses one or two steps of iterated dominance. 35, or guess that others will choose 35 and choose 25. Very few subjects chose That is, most subjects roughly guess that the average will be 50 and choose First-round choices are around 21-40. A careful statistical analysis indi-

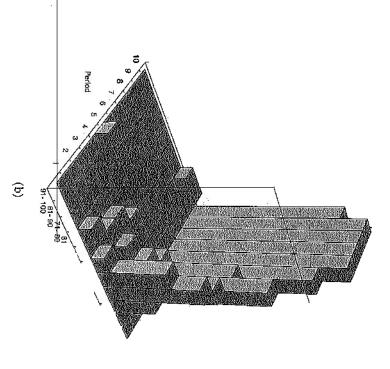


Figure 1.3 (continued)

across rounds. understand initial choices and a theory of learning to explain movement Behavioral game theory uses a concept of limited iterated reasoning to initial choices, players are inexorably drawn toward zero as they learn. Although the game-theoretic equilibrium of zero is a poor guess about

Chapter 5 for details), including Caltech undergraduates, 12 trustees on The beauty contest has been replicated in dozens of subject pools (see

Generally they do not play much differently than students at other colleges. how these students play simple games establishes whether very analytical students can figure the games out the applicants have been higher than the average of those students who are easepted at Harvard. Studying years, the incoming first-year class has a median math SAT score of 800. Recently, the average test scores of 12 Caltech students are a useful subject pool because they are extraordinarily analytically skilled. In many

The limited iterated reasoning measured in these games provides one explanation for persistence of phenomena such as the stock price bubbles Keynes had in mind. Even if all investors foresee a crash, they do not "backward induct" all the way to the present. They guess that others will sell a couple of steps before the crash, and plan to sell just before that exodus. This reasoning process does not unravel all the way (because doubt "reverberates"), which explains why bubbles can persist even if everyone knows they will eventually burst. Allen, Morris, and Shin (2002) make their argument precise and Camerer and Weigelt (1993) and Porter and Smith, (1994) show that bubbles can happen in the lab.

1.3 Experimental w _ .u. iv, iv. u. u. u.

This book is a l

Consider the three examples above. In ultimatum bargail..., In lar from the perfect equilibrium-assuming self-interest, but they have been equilibrium when the Responder's preference for being treated

fairly is taken into account (because offers maximize expected profit gives because rejection rates). Behavioral game theory explains these results he can be an expected profit gives be continental divide and beauty contest games, players start far from equilibrium and converge close to it in ten periods or so. Behavioral game theory explains these results using concepts of limited reasoning as players first think about a game (see Chapter 5) and precise theories of learning (see Chapter 6).

Sherlock Holmes said, "Data, data! I cannot make bricks without clay." Experimental results are clay for behavioral game theory. The goal is not to "disprove" game theory (a common reaction of psychologists and sociolo-

1.3 Experimental Regularity and Behavioral Game Theory

gists) but to *imp*rove it by establishing regularity, which inspires new theory. Without some sort of observation, theoretical assumptions are grounded in casual pseudo-empirical work—informal opinion polls in seminar and office discussions and using one's own intuitions (a one-respondent poll). Biologists don't just ask "If I was a robin foraging for food, how might I do it?" They watch robins forage, or ask somebody who has. Theorist (and part-time experimenter) Eric Van Damme, among others, worries about the effects of having too few data of this sort in game theory (1999, p. 204):

Without having a broad set of facts on which to theorize, there is a certain danger of spending too much time on models that are mathematically elegant, yet have little connection to actual behaviour. At present our empirical knowledge is inadequate [precisely the same word you Neumann and Morgenstern used fifty years before!] and it is an interesting question why game theorists have not turned more frequently to psychologists for information about the learning and information processing processes used by humans.

than one equilibrium (see Chapter 7) and how equilibration occurs in feetly understood (see Chapter 6). Pure mathematics alone will not live these problem

il recently? One possibility is that early experimentation was thought have "failed." In a 1952 RAND conference, several theorists (including Nobel laureate Nash) gathered to think about game theory. They is did some experiments, the results of which did not confirm theory and in data also suffered from the fact that so many interesting mathematical ferom about 1970 onward, developments in the theory of repeated from the factory and applications to important fields such as principal—agent relations, contracting, and political science led

¹³ I think these early experimenters made a mistake by concentrating too much on games with mixedstrategy equilibria. In those games, players have low monetary incentives and predictions depend on assumptions about risk tastes, which are difficult to measure or even control.

[&]quot;Many "modern" ideas in behavioral game theory were first proposed early in the finitory of game theory, and left aside or forgotten. In his thesis Nach (1950) described a "mass action" interpretation of equilibrium similar to modern evolutionary game theory (Weibull, 1995). Weighted fictitious play (see Chapter 6), which seems to have been revived by empiricists around 1995, is described in the amazingly insightful book by Luce and Raiffa (1957). Solten (1978) emphasized how players perceive the game they play, a topic being revived by Rubinstein (1991), Cameter (1999), and Samuelson (2001), among others. Rosembal (1989) first proposed a "quantal response equilibrium" version, later refined and applied by McKelvey and Palfrey (1995, 1998) and Goerce and Holt (1999).

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serious attention to modeling bounded or procedural rationality formally observation to theory. It is also encouraging that some theorists have turned of any sort. There is also little doubt that it is high time to raise the ratio of (e.g., Rubinstein, 1998).15 insightful and necessary, but it was conducted with little empirical guidance explosion of theory. There is no doubt that this pursuit has been extremely

p. 208); and theorizing working together is summarized by Vince Crawford (1997, important too.16 The result of controlled experiments, field observation, game theory. Detailed facts about cognitive mechanisms and field tests are Of course, experimental data are only one component of behavioral

cal frameworks for analyzing games-traditional non-cooperative game but that most behavior can be understood in terms of a synthesis of tive learning models—gives a fully reliable account of behavior by itself, theory, cooperative game theory, evolutionary game theory, and adapproportions that depend in predictable ways on the environment ideas from those frameworks, combined with empirical knowledge in The experimental evidence suggests that none of the leading theoretic

Rapid development of behavioral game theory will depend on how scientists react to data. Reactions vary.

understanding from data, there is no way to falsify the theory. Physicists and understood. Resist this conclusion. The games are usually simple, and most minded to what behaving humans can teach them about human behavior. survival?] they would get it right!"). Game theorists should be similarly openbirds didn't forage for food as predicted ("If they had more at stake [than biologists would not have the same reaction if a theory about particles were subjects know how choices lead to payoffs. Furthermore, by inferring subject experimenters carefully control for understanding by using a quiz to be sure must have understood; if the data disconfirm, the subjects must have not were motivated. If the data confirm game theory, you might say, the subjects falsified by careful experimentation ("The particles were confused!") or if take the data as simply showing whether subjects understood the game and If you are smitten by the elegance of analytical game theory you might

a key element of behavioral game theory—namely, that equilibration may crucial component of any theory). In the foreword to Roth and Sotomayor's take a long time, perhaps years or decades (and equilibration is therefore a In fact, evidence cited as confirmation of game theory often supports

cian Robert Aumann notes that

down, the payoff is not five dollars but a successful career, and people fare quite well have time to understand the situation—the predictions of game theory more than half a century. . . . in the real real world—when the chips are use already since 1951 for the assignment of interns to hospitals in the United States; it had evolved by a trial-and-error process that spanned the Gale-Shapley [matching] algorithm had in fact been in practical

years117 Over such a span, a learning or equilibration theory is essential. Note that the "time to understand the situation" Aumann refers to was fifty

design. Aumann, again, writes (1990, p. xi): Another reaction you may have is to criticize details of experimental

scriptions. To back up such assertions, some workers have conducted world," that people don't really behave according to game-theoretic preexperiments represented the real world. derstand what they are about and are paid off by pittances; as if such experiments using poorly motivated subjects, subjects who do not un-It is sometimes asserted that game theory is not "descriptive" of the "real

students who are quizzed and highly motivated designed with them in mind. Subjects are typically analytically skilled college from the past ten years—fully respect concerns such as Aumann's and are in Chapter 3). The modern experiments described in this book-mostly Aumann is alluding to an earlier generation of experiments in the 1960s and This book largely ignores those experiments (though some are described 1970s which were not sensitive to subject comprehension and incentives

for robusiness create one-shot games, and variation in stakes and subject pool to check to ensure subject comprehension, control for anonymity when trying to bristle when they are made in ignorance of the extraordinary care taken be tested and falsified. However, these explanations make experimenters than the experimenter created. Such explanations are useful if they can to analytical game theory is that subjects were playing a different game Another reaction you are likely to have when behavior does not conform

information structures, and so on. Most of this work is not directly inspired or disciplined by data, however. ¹⁵This includes finite automata, e-equilibrium, evolutionary and dynamic theories, non-partitional

impressive examples (e.g., Roth and Xing, 1994). 16 Roth's work on matching for college bowl games, sorority rush, and medical residency are rare,

to play equilibrium strategies." But the learning was on the order of decades, which means a behavioral batting averages converged in the 20th century because of dynamic adjustments in field, pitching, and learning theory is just as important (or more so) than an equilibrium concept. hitting. Dixit and Skeath describe this as an "encouraging tale, drawn from real life, of how players tearn 17 A similar point is made by Dixit and Skeath (1999). Stephen Jay Gould (1985) argued that baseball

For example, a common interpretation of the fact that Responders reject offers in ultimatum games is that the Responders think they might be playing a repeated game because they will meet the Proposers again. But experimenters go to great lengths to ensure that subjects won't meet again and know that. For example, some experimenters pay subjects one at a time, with a short lag between each payment, and stand in the hall to be sure subjects don't wait for others to leave. Under these conditions, the faux-repeated-game explanation of ultimatum results is simply wrong. Others (such as the famously careful Ray Battalio) are known to end an experiment immediately if a subject says something aloud that others hear, breaking the experimenter's control. The reaction that subjects are playing a different game than the experimenter intended should disappear as more theorists learn about what actually happens in laboratories and come to believe in the quality of the data that are produced.

Still another reaction you may have is that behavior which is not rational can't be modeled. For example, several years ago Abreu and Matsushima (1992b) said experimental results are frequently inexplicable by "even approximately rational explanation." I disagree: Virtually all the results reported in this book can be accommodated by including behavioral components—social utility, limited iterated reasoning, and learning—into analytical theory. They go on to ask, "Should we then give up the rationality paradigm?" Of course not. It is too useful as a source of sharp predictions, and it is often a good prediction of limiting behavior. Behavioral game-theory extends rationality rather than abandoning it. The last chapter of this book shows how.

1.4 Conclusion

This chapter described three examples which illustrate experimental regularity, and hinted how that regularity is formalized in behavioral game theory.

In the ultimatum game, Proposers typically offer close to half of a sum to be divided, and Responders reject offers that are too low because they dislike unfairness. The game is so simple that it is impossible to believe Responders rejecting money are confused, and the result has been replicated for very high stakes (up to \$400 in America, and comparable sums in foreign countries). According to behavioral game theory, Responders reject low offers because they like to earn money but dislike unfair treatment (or like being treated equally). In the continental divide game, players gravitate toward equilibria over time and often end up in Pareto-inefficient equilibria they could have avoided. Behavioral game theory explains this by assuming that players aren't sure what to do (at the beginning of the game), so they

pick numbers in the middle; then they respond to history according to simple statistical learning rules. In the beauty contest game, players seem to do one or two steps of reasoning about others, then stop. (Analytical game theory assumes they keep going until they reach a mutual best-response equilibrium.) And they learn over time. Later chapters expand on these results and describe other classes of games (mixed equilibria, bargaining, signaling, and auctions).

APPENDIX

Al.1 Basic Game Theory

This appendix introduces basic ideas in game theory. ¹⁸ The goal is to equip the novice reader to understand the gist of the rest of the book. If you do not have some other background in game theory, and are serious about understanding the experimental results described later, you should read other books. A good introductory book (low on math) is Dixit and Skeath (1999). More mathematical books include Rasmusen (1994) and Osborne and Rubinstein (1995). Gintis (1999) includes fresh material on evolutionary theory and experimental data, and tons of problems. The heavy tomes that are used in graduate classes at places such as Caltech include Fudenberg and Tirole (1991).

Notation: Player *i*'s strategy is denoted s_i . A vector of strategies, one for each player, is denoted $s = s_1, s_2, \ldots, s_n$. The part of this vector which removes player *i*'s strategy (i.e., every other player's strategy) is denoted s_{-i} . The utility of player *i*'s payoff from playing s_i is $u_i(s_i, s_{-i})$.

A1.1.1 Dominance

Definition A1.1.1 The strategy s_i^* is a dominant strategy if it is a strict best response to any feasible strategy that the others might play

$$u_i(s_i^*, s_{-i}) > u_i(s_i', s_{-i}) \ \forall s_{-i}, s_i' \neq s_i^*$$

The strategy s_i' is dominated if there exists $s_i'' \in S_i$ such that

$$u_i(s_i'', s_{-i}) > u_i(s_i', s_{-i}) \ \forall s_{-i}.$$

¹⁸Thanks to Angela Hung for writing much of this appendix.

A1.1 Basic Game Theory

I Introduction

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The strategy s_i' is weakly dominated if there exists $s_i'' \in S_i$ such that

$$u_i(s_i'', s_{-i}) \ge u_i(s_i', s_{-i}) \ \forall s_{-i},$$

 $u_i(s_i'', s_{-i}) > u_i(s_i', s_{-i}) \text{ for at least one } s_{-i}.$

Example A.I.I.I Consider the simple normal-form game below. In a normal-form (aha strategic-form or matrix) game players are presumed to move simultaneously so there is no need to express the order of their moves in a graphical tree (or extensive-form). Each cell shows a pair of payoffs. The left payoff is for the row player (1) and the right is for the column player (2). The payoffs are utilities for consequences. That is, in the original game the consequences may be money, pride, reproduction by genes, territory in wars, company profits, pleasure, or pain. A key assumption is that players can express their satisfaction with these outcomes on a numerical utility scale. The scale must at least be ordinal—i.e., they would rather have an outcome with utility 2 than with utility 1—and when expected utility calculations are made the scale must be cardinal (i.e., getting 2 is as good as a coin flip between 3 and 1).

b

For player 2, strategy R is strictly dominated by M (because M gives a higher payoff if player 1 chooses U, 2 instead of 1, and a higher payoff if player 2 chooses D, 1 instead of 0). Deleting strategy R (i.e., assuming a rational player 2 will never play it) makes D strictly dominated by U. But if player 1 plays U, then player 2 should play M. Therefore, the iterated-dominance equilibrium is (U,M).

Dominance is important because, if utility payoffs are correctly specified (one need get only their order right) and players care only about their own utility, there is no good reason to violate strict dominance. One step of iterated dominance is a judgment by one player that the other player will not make a dumb mistake. This often tells a player what she herself should do. In the example, player 1 might consider choosing D because of the chance of earning the 2 payoff in the lower right (D,R) cell. But will she ever earn that payoff? Only if player 2 does something that is dominated. If player 1 assumes player 2 won't do that, she can rule out R, and her hope of earning 2 disappears. Then she should obviously choose U.

Example A1.1.2 (Battle of the Sexes)

Player 2 $L \qquad M$ $D \qquad \begin{array}{c|c} Player 2 \\ L & M \\ \hline 0,0 & 1,2 \\ \hline \end{array}$

The game is not dominance solvable. Neither strategy is dominant (or dominated) for either player because there is no one strategy that is always best. Put differently, each strategy might be best depending on what you think the other person will do.

A1.1.2 Nash Equilibrium

Definition A1.1.2 The strategy profile $s^* = (s_i^*, s_{-i}^*)$ is a Nash equilibrium (NE) if each player's strategy is a best response to the other players' strategies. That is, no player has incentive to deviate, if no other player will deviate. (If players find themselves in equilibrium, there is no reason to move away.)

$$u_i(s_i^*, s_{-i}^*) \ge u_i(s_i', s_{-i}^*) \ \forall s_i'i.$$

Note that, if a strategy profile is an iterated-(strict) dominance equilibrium,

application of weak dominance

Example A1.1.3 (Battle of the Sexes) Solving for pure-strategy Nash equilibrium:

	Player I		
D	U	ř	
0,0	2,1	L	Pla
1,2	0,0	R	Player 2

If player 1 plays U, 2's best response is L. If player 1 plays D, 2's best response is R. If player 2 plays L, 1's best response is U, and if 2 plays R, 1's best response is D. Therefore, U is a best response to L, and L is a best response to U. Likewise, D is a best response to R and R is a best response to D: Pure strategy NE are (U,L) and (D,R).

A1.1.3 Mixed Strategies

A mixed strategy for player i is a probability distribution over all the strategies in S_i .

A.l. I Basic Game Theory

Example A1.1.4 (Battle of the Sexes) Solving for mixed strategy Nash equilbrium:

	Player 1	•	
D	\boldsymbol{u}		
0,0	2,1	L	Pla)
1,2	0,0	73	Player 2
:	٠.	•	

2 plays L with probability q and R with probability 1-q. Suppose player 1 plays U with probability p and D with probability I-p and player

Then the expected value to 2 from playing L is

$$\mathrm{I} p + 0(1-p)$$

and the expected value to 2 from playing R is

$$0p+2(1-p).$$

Player 2 is indifferent iff

$$1p + 0(1 - p) = 0p + 2(1 - p)$$

ş

The expected value to 1 from playing U is

$$2q + 0(1-q)$$

and the expected value from playing D is

$$0q + 1(1-q)$$
.

Player 1 is indifferent iff

$$2q + 0(1-q) = 0q + 1(1-q)$$

9

As a result, a pair of (weak) best responses constitutes a mixed-strategy equilibrium. $\left(\left(\frac{2}{3}U,\frac{1}{3}D\right),\left(\frac{1}{3}L,\frac{2}{3}R\right)\right).$

> what will happen will always have something concrete to sav. equilibrium. This means that a policy analyst or scientist trying to predict ductive: For any (finite) game you write down, you can be sure to find an existence is a beautiful thing and is part of what makes game theory proguarantee existence of a Nash equilibrium (in finite games). Guaranteed space, all points in between are in the space too), which is necessary to strategies makes the space of payoffs convex (i.e., for any two points in the Mixed-strategy equilibrium is a curious concept. Introducing mixed

predicted probabilities, the mixed equilibrium is a mutual best-response as long as each player's belief about the other players' choice matches the equilibrium (called "purification") is that one player might appear to be point. Chapter 3 gives more detail. variable they privately observe. Mathematically, this works the same waymixing but is actually choosing a pure strategy conditional on some hunch player's payoffs, which is odd. A modern interpretation of mixed-strategy one player's equilibrium mixture probabilities depend only on the other particular probabilities; she just doesn't care what she does. Furthermore, pure strategies, which means she does not (strictly) desire to mix with By definition, a player desires to mix only when she is indifferent among However, the behavioral interpretation of mixing strategies is dubious.

		Player I		
B(1-p-q)	M(q)	T(p)		
35,100	40,50	30,30	L(r)	
60,10	45,45	50,40	M(s)	Player 2
0,0	10,60	100,35	R(1-r-s)	.5

Player 1:

2

$$30r + 50s + 100(1 - r - s) = 40r + 45s + 10(1 - r - s)$$

= $35r + 60s + 0(1 - r - s)$,

Because the game is symmetric,

$$p = r = \frac{22}{83},$$

$$q = s = \frac{56}{83},$$

$$1 - p - q = 1 - r - s = \frac{5}{83}.$$

Al.1.4 Constant-Sum Games

stant. For two-person, constant-sum games, minimax, maximin, and Nash money or food-sharing) the players' utilities probably do not add to a coneven when the sum of physical payoffs is constant (like bargaining over equilibrium all select the same strategy. across outcomes. Constant-sum games are actually extremely rare because In a constant-sum game, the sum of the payoffs of the players is constant

possible payoff; that is, Definition A1.1.3 The strategy s_i^* is a maximin strategy if it maximizes i's minimum

Definition A1.1.4 The strategy s_i^* is a minimax strategy if it minimizes the other players' maximum possible payoff; that is,

$$s_i^* = \arg\min_{s_i} \left[\max_{s_{-i}} u_{-i} \right]$$

Example A1.1.6 (Matching Pennies)

the row player I is to randomize equally over U and D, which gives an expected utility expected utility). It is also the unique Nash equilibrium. of 0.5 for both L and R. Hence, 0.5 is the maximin value. It is also the minimax strategy because it guarantees that the column player 2 makes no more than 0.5 (in If the game is expanded to include mixed strategies, then the maximin strategy for

A.I. I Basic Game Theory

strictly opposed. If you best-respond, I'll get the least; my best response to that likelihood is to maximize the least I can get. will necessarily give you the lowest payoff, because the players' interests are fact that the other player's best responsiveness (as in Nash equilibrium) In constant-sum games, minimax is a heuristic way of respecting the

A1.1.5 Extensive-Form Games and Information Sets

information sets; and (5) utility payoffs at each end node. choose branches at random nodes; (4) collections of nodes, which are called to each player; (3) probabilities that "nature" (an outside force) uses to node to its end (terminal) nodes; (2) an indication of which node belongs and branches running without any closed loops from a single (root) starting order of moves. An extensive-form game is (1) a configuration of nodes An extensive-form game is used to model games where there is a specific

satisfying: Definition A1.1.5 An information set for a player is a collection of decision nodes

- 2 1

Al.1.6 Subgame Perfection

my view, this "refinement" of Nash equilibrium simply patches up an omis sion in Nash's concept, which was not evident until theorists began thinking uation game from a singleton node—i.e., a node which has no other nodes about extensive-form trees rather than matrices. in its information set—to the end nodes which follow from that node.) In strategy if the subgame is reached (Selten, 1965). (A subgame is the continposes the further restriction that players will actually play their equilibrium do at each information set, even those not reached. Subgame perfection im-An equilibrium for an extensive-form game specifies what each player will

Example A1.1.7 Mini-ultimatum game

In this mini-ultimatum game, player I moves first and offers an even (E) split of 10, paying (5,5), or offers an uneven (U) split. If E is chosen, the game ends and both players earn 5. If U is chosen, player 2 is "on the move" and can choose to accept (A), in which case player I gets 8 and player 2 gets 2, or can reject (R), in which case both get nothing.

The strategy profile (E, RIU) is a Nash equilibrium because it specifies moves at each node, and strategies are—technically—best responses. If player 1 anticipates that player 2 will choose R after a move of U, then player 1 should choose E to earn 5. And if player 1 is going to choose E, it makes no difference what player 2 does—"planning" to respond with R to U is not penalized because, in equilibrium, player 2 is never called upon actually to play. Playing U after R is a weak best response because in this equilibrium R never results. Subgame perfection requires that, if the U node is reached, then player 2's subsequent strategy must be a best response. But since R earns 0 for player 2 and A earns 2, the best response in the subgame that results when player 1 chooses U is to play A. Anticipating this, player 1 should choose U. Therefore, (U, AIU) is a Nash equilibrium and is also subgame perfect.

A1.1.7 Bayesian-Nash Equilibrium

an off-path move has probability zero (i.e., $P(D|H_i) = 0 \text{ V}H_i$). Then the detheir beliefs about player types using Bayes' rule. Bayes' rule states that $P(H_i|D) = P(D|H_i)P(H_i)/\sum_k^n = 1P(D|H_k)P(H_k)$, where H_i are n different However, the probability distribution of types is common knowledge (the which branch emanating from the start node nature chose. The player who the types of others. (In formal terms, the player who knows her type knows and determine a player's "type." Players observe their own types but not Harsanyi, 1967-68) by having "nature" move at the beginning of the game nominator of the updating equation is zero and Bayes' rule breaks down. well that Bayes' rule does not restrict what these beliefs should be, because cur in equilibrium), players should have some belief about player types. Note player's move). (ii) Off the equilibrium path (i.e., after moves that never ochypotheses (e.g., possible player types) and D is the observed data (e.g., a that occur in equilibrium with positive probability), players must update to Nash equilibrium: (i) Along the equilibrium path (i.e., for all moves "common prior" assumption). Bayesian-Nash equilibrium adds two features nodes that emanate from both branches following from the start node.) does not know the other player's type has an information set containing the other players' payoff function(s). This is traditionally represented (after In games of incomplete information, at least one player is uncertain about Hence, Bayesian-Nash equilibrium imposes the minimal a-Bayesian restric-

tion on what off-path beliefs should be—namely, they should be something! This simply rules out the possibility that players will violate dominance after observing an off-path move.

A1.1.8 Trembling Hand Perfection

strategies are larger, leading to a concept of "proper" equilibrium. Some precise). Myerson (1978) suggested that the tremble probabilities should be equilibrium (Kreps and Wilson, 1982a) is a kissing cousin of trembling hand smaller when payoff differences between equilibrium and nonequilibrium two differ are knife-edge cases, in a way that can be made mathematically perfection and is generically the same (i.e., the only games in which the sort of beliefs after off-path moves seem intuitive or sensible. Sequential others have suggested further refinements which try to codify, logically, what Nash equilibria with trembling, as the tremble probability goes to zero. Many are taken with positive probability. Then Bayes' rule can be used to update other refinements are discussed in Chapter 8, on signaling games beliefs. A trembling hand perfect equilibrium is the limit of the Bayesianplayer's hand trembles when she chooses, so that all paths through the tree idea is to suppose that, even in an equilibrium, there is a small chance that a to the discipline of Bayes' rule, called "trembling hand perfection." The Selten (1975) suggested a clever way to subject off-equilibrium-path beliefs

A1.1.9 Quantal Response Equilibrium

In a quantal response equilibrium (QRE), players do not choose the best response with probability one (as in Nash equilibrium). Instead, they "better-respond," and choose responses with higher expected payoffs with higher probability. In practice, the QRE often uses a logit or exponentiated payoff response function:

$$P(s_{i}) = \exp\left(\lambda \sum_{s_{-i}} P(s_{-i}) u_{i}(s_{i}, s_{-i})\right) / \sum_{s_{k}} \exp\left(\lambda \sum_{s_{-i}} P(s_{-i}) u_{i}(s_{k}, s_{-i})\right),$$

where $\exp(x)$ denotes e^x and the sums are taken over all strategies for -i (all other players) and i. Intuitively, QRE says that players fix a strategy and form beliefs about what others will do $(P(s_{-i}))$, and compute expected payoffs given those beliefs. Making this calculation for each strategy gives a profile of expected payoffs for each possible strategy. Then player i betterresponds by choosing noisily according to the strategies' expected payoffs. The parameter λ is a measure of their sensitivity to differences in expected.

Introduction

payoffs. ¹⁹ Note that since player I is calculating $P(s_i)$, and others are too, the system of equations is recursive: A player's behavior determines expected payoffs, which determine other players' behavior. When $\lambda=0$, players just choose each strategy with the same equal probability. As λ rises, they become more and more responsive, converging to Nash equilibrium in which they always choose the best response. ²⁰ Thus, Nash equilibrium is a kind of "hyperresponsive" QRE.

response model of bargaining just recently; so we can count him as recently truth and said "Nash didn't deny that he would have discovered QRE." Still speculation about his would-be early discovery of QRE, I later stretched the in the audience! Since Nash didn't protest when he heard my counterfactual were grinning and nudging because, unbeknownst to me, Nash had been quired the development, much later in the 1960s and 1970s, of subgame and presolved the problem of refining away incredible Nash equilibria, which rethan Nash equilibrium. (Such an early discovery would have automatically tician rather than a mathematician, he might have discovered QRE rather blank about QRE. He said he had been working on a similar stochastic best later, in December 2001, I had a chance to meet Nash and asked him point (Nash was, after all, a hometown hero in Princeton). People later said they in the fall of 2001, some audience members grinned and nudged each other trembling-hand perfection.) When I mentioned this at a talk in Princeton converted to, or at least sympathetic toward, a quantal response approach I used to say in classes and seminars that, if John Nash had been a statis

Al.2 Experimental Design

The way in which an experiment is conducted is unbelievably important. Just as all thoroughbred racehorses are descended from four horses, most American experimental economics began in the 1960s and 1970s at a small number of institutions (particularly Caltech, Arizona, Purdue, and Texas A&M) and grew slowly. (A similar effort occurred in parallel in Germany.) As a result, the experimental community is tight-knit and has established clear conventions for experimental practice which permit a high degree of comparability across data sets. Smith (1976) is an early rulebook which also summarizes many regularities. For example, most articles include raw data and instructions to enable readers to judge for themselves what was learned. (If you asked a psychologist for data or instructions he or she might

be insulted, because the convention in that field is to give the writer the benefit of the doubt.)

This appendix sketches some important design choices. To learn more, see Friedman and Sunder (1993), Davis and Holt (1993), and Kagel and Roth (1995).

A1.2.1 Control, Measure, or Assume

Any variable can be evaluated in one of three ways: control, measurement, or assumption.

Control means taking an action to affect the value of a variable, often with a "manipulation check" to be sure the control worked. Induced value is an important kind of control which creates preferences for actions by associating those actions with payoffs in a currency that subjects value (typically money, but sometimes grade points, ranking of points earned, and so forth).

Measurement refers simply to measuring the value of a relevant variable through psychometric measures ("Describe how angry you are when someone offers you \$2 out of \$10?"), methods for measuring risk-aversion (e.g., certainty equivalents) or probability judgments (scoring rules). Types of measurement that are less familiar in economics, but worth exploring, include content analysis of videotapes, physiological measures such as heartrate or galvanic skin response, information acquisition (see Johnson et al., 2002, in Chapter 4, and Costa-Gomes, Crawford, and Broseta, 2001, in Chapter 5), and even fMRI brain imaging (Smith et al., 2002).

Assumption is pseudo-control in which the experimenter is willing to accept a maintained hypothesis about the value of a variable.

Substitute and fraging

As an illustration of all three methods, consider the classic economic experiments in which agents are endowed with costs and valuations for an object, and one would like to test theories of competitive equilibrium (CE), which predict that prices will converge to the point where supply meets demand. One strategy is to hand out everyday objects, such as CD recordings or coffee mugs, and make an assumption about how much subjects value them. This is generally a bad design because CE predictions are very sensitive to the valuations of marginal traders, and the valuations are not likely to be well understood by experimenters. ²¹ Another strategy is to

¹⁹Goeree and Holt (1999) use $1/\mu$ instead to emphasize their interpretation of the noise as computational mistakes; when μ is large, the mistake rate is high and players are very insensitive, and vice versa.

²⁰This is not quite true, technically. The limit of a sequence of QREs as \(\lambda\) increases can converge to something that is not a Nash equilibrium (see McKelvey and Palfrey, 1995).

²¹A beautiful exception, which proves the rule, is the Kahneman, Knetsch, and Thaler (1990) experiments with coffee mugs. They were interested not in prices at all, but only in the quantity of trade, and in showing that aversion to losses creates an "endowment effect" that is present with everyday objects and not with induced-value tokens. They were able to use everyday objects because they did not care about the level of homemade valuations, but needed only to assume that mean valuations were similar in samples that (randomly) did and did not receive mugs.

A1.2 Experimental Design

measure valuations for each individual (using, say, the incentive-compatible Becker–DeGroot–Marschak procedure) and then assume those measured valuations represent the subjects' costs and reservation prices and construct demand and supply curves from the measurements. This is a defensible procedure but has rarely been used (see Knez and Smith, 1987). A third strategy is to "induce" or control valuations by making the objects of trade valueless tokens, and telling subjects that they can trade tokens for specific money values. This form of induced valuation, first used by Chamberlin (1948) and tirelessly refined by Vernon Smith beginning in 1956, is surely the crux move in the development of experimental economics. Smith's later insistence on actually tying money payments to the induced valuations led to credibility among nonexperimenters and reliability in actual behavior, which enabled exploration of extremely subtle hypotheses and rapid progress.

A1.2.2 Instructions

Instructions tell subjects what they need to know. It is scientifically very useful to have a clear instructional "script" that enables precise replication, particularly across subject pools who may vary in language comprehension, obedience, intrinsic motivation, and so on. (Precise replication is surprisingly rare in other social sciences, in psychology for example.) Reading instructions out loud is a common practice to establish "public knowledge" (e.g., what subjects know everyone else has been told, and what everyone else knows everyone else has been told), which is as close as we can practically come to the common knowledge usually assumed in game theory.

The overwhelming convention in modern (post-1975) game theory experiments is to explain how each sequence of moves by each player leads to payoffs (including payoffs to other subjects, and also including asymmetric information à la Harsanyi). This practice arose because experimenters wanted to be sure that subjects had enough information to compute an equilibrium. (Earlier experiments on markets deliberately withheld information about values of others, to test the Adam Smith/Hayek hypothesis that, even if players knew only their own values, they could still converge to a Pareto-efficient equilibrium.) More recently, learning models have been proposed that do not always assume players have complete knowledge of all possible payoffs. As an empirical matter, it is quite interesting to know how people learn in these environments (since players may have poor information about payoffs in many naturally occurring situations). So some recent experiments have deliberately withheld information about payoffs from the instructions (e.g., Van Huyck, Battalio, and Rankin, 2001). This design choice also raises

a problem—when subjects are not told something about the environment they are placed in, their default assumption may be wrong.

it will be difficult to conclude whether subjects are playing rationally or not the guesses are hard to observe directly (without additional measurement), no guarantee that subjects will guess accurately what they are not told. Since choice. But, by not revealing information about the environment, there is choosing. Withholding statistical information is not necessarily a bad design a mistake (they should always choose the arm with the higher p). Does the process was independent and identically distributed, this would be perceptions about the statistical process of reward and their decision rule for probability-matching experiment is a combination of the subjects' revealed has placed them in? What the experimenter observes in a low-information they fail to guess the strange (uninteresting) environment the experimenter probability matching tell you that subjects are making a mistake, or that "probability match" by choosing L on about p of the trials. If subjects knew experimenter is interested in whether they can figure out an elaborate are delivered. It might be much more plausible, to a subject, that the L has an independent p chance each time. Empirically, subjects typically pattern of variation in which levers are armed rather than figure out that (with fixed p), they might entertain an array of possibilities of how rewards told that the lever-arming process is independent and identically distributed are independent Bernoulli trials. But what do subjects think? If they are not and the other delivers nothing. Subjects choose one lever and receive a and right R). On each trial one of the levers is "armed" to deliver a reward subjects (including nonhuman animals) making one of two choices (left L reward if it is armed. Typically, there is a chance p that L is armed and *previous trials*. From the experimenter's view, the rewards from choosing L - p that R is armed, and which lever is armed is determined independently of Here is an example. A large literature on "probability matching" studies

11.2.3 Anonymity

If the subjects know the identity of the person they are bargaining with, their knowledge might influence what they do for many reasons. They might like the way the person looks and want to make them happy, or fear retribution or embarrassment if they make a stingy offer and see the person after the experiment. Unless these possibilities are precisely the focus of the experiment, most of the experiments described in this book try to create anonymity—sometimes to a dramatic degree—by making it as difficult as possible for subjects to know precisely who they are playing with. Anonymity is obviously not used because it is lifelike. It is used to establish a benchmark

A1.2 Experimental Design

against which the effects of knowing who you are playing can be measured, if those effects are of interest.

A1.2.4 Matching Protocols and Reputation Building

Experiments are usually designed with several periods of play so subjects can learn from experience. But if a pair of subjects play together several times, the possibility of "reputation building" can affect the prediction that game theory makes. For example, in the ultimatum game it may pay for a Responder to build up a reputation for being "tough" by rejecting large offers in the first few periods, to "teach the proposer a lesson" and get larger offers in later periods. Put more formally, when the same pair (or group) of players play together several times, there may be game-theoretic equilibrian for the repeated game that differ from the one-shot, stage-game equilibrium. Unless we are explicitly interested in the nature of reputation formation and repeated-game strategies (as some experiments are), this possibility is avoided by having subjects play with each other only once in an experimental session.

There are various ways in which players can be matched with different players in a stage game that is repeated. The most common protocol is no-repeat rematching (or a "stranger" design)—players are never rematched with a former match, to reduce the possibility of reputation building. (It is not known, by the way, whether no-repeat rematching actually does disable reputation building. I suspect it does not, but more work on this is needed.) In a "no-contagion" design, players are never rematched, and are never rematched with somebody who will be matched with somebody they will later be matched with, and so forth. In random rematching, players are rematched randomly (so they may be rematched with their partner from the previous period, but typically the probability of consecutive matches is low and they do not know whether they are rematched anyway). In a meanmatching or population protocol, each player playe every other player and earns the average payoff from all those matches.

A1.2.5 Incentives

Vernon Smith (1962) reported the earliest experiments comparing the behavior of subjects who were rewarded in points with that of subjects whose points were converted into dollars that they were actually paid. Vernon observed that subjects paid only in points tended to approach competitive equilibrium more erratically, and seemed to grow bored with the experiment faster than those who were paid money. He suggested that, although people may have enough intrinsic motivation to earn lots of points, hypothetical rewards were typically more "erratic, unreliable, and easily satiated"

(1976) than money. Put differently, by inducing value using money payments, the experimenter need rely only on the assumptions that everybody likes having more money and nobody gets tired of having more of it. These are safe assumptions, and substantially safer than figuring out whether somebody is motivated by having their name posted if they did best (some people might be embarassed by it), is likely to give up if they are far behind when payoffs have a tournament structure, and so forth. (If you know anybody who is tired of getting more money let me know; I'll take their leftovers!)

in tasks that are quite easy ("floor effects") or very hard ("ceiling effects") can have comparably large effects and should be investigated further. are returns to thinking harder (see also Hertwig and Ortmann, 2001). But formance most reliably in judgment and decision-making tasks, when there just as large. Labeling strategies, individual differences, and other variables pirical reason to obsess only about money, because the effect of experience is paying money usually does not matter. We also point out that there is no emthat are sensitive to variation, such as "weak-link" coordination games (see tasks investigators should certainly pay money.) Paying money improved per Chapter 7) or asset markets with potential for speculative bubbles. (In those duce variation and outliers, which may be particularly important in settings more thorough review and draw several conclusions. Paying money does recouple of dozen studies and argue that paying money reduces variance of reworking paper). Hogarth and I (Camerer and Hogarth, 1999) conducted a sponses around a rational prediction (first noted by Dave Grether in a 1981 been overturned by paying more money. Smith and Walker (1993) review a dence is mixed. Experimenters should not abandon the practice of paying with important exceptions such as Ward Edwards and Amnon Rapoport). economics (in sharp contrast to most of modern experimental psychology, performance-based incentives, but few results that disconfirm theory have Does it matter whether performance is rewarded, and how much? The evi-Paying subjects their earnings quickly became the norm in experimental

14 2 3 1 J

In the 1980s a controversy erupted over whether money payments established what Vernon Smith called "dominance," which means that the money at stake is enough to induce subjects to think hard. The controversy was ignited by Harrison (1989), who pointed out that the size of a deviation from theory in payoff terms may be much lower than the deviation in the strategy space. (The same point—the "flat maximum critique"—was made almost two decades earlier, in 1973, by Von Winterfeldt and Edwards.) For example, in a mixed-strategy equilibrium, if other players are using their mixture strategies, then a subject has absolutely no financial incentive to play her equilibrium mixture instead, regardless of the level of money payoffs in the game. Similarly, in first-price private-value auctions, a bidder who overbids by, say, \$1 does not actually lose a dollar. Overbidding reduces her prospective earnings but raises the chance of winning the auction, and the net effect may reduce her expected payoff by only pennies.

A1.2 Experimental Design

Experimenters never developed an ideal solution to the flat maximum problem. The critique did sensitize us to the need to worry about marginal costs of deviation (and see Fudenberg and Levine, 1997) and to seek designs with steep marginal incentives where possible. (For ultimatum game Responders, for example, the cost of the error from rejecting is exactly equal to the deviation in strategy space, and is often very large.) Furthermore, the fact that very large variations in stakes typically have only modest effects muted criticisms that payoffs were not large enough. At least two dozen studies have been done in foreign countries where purchasing power is so low that modest sums by the standards of developed countries amount to several weeks' or months' earnings. The results are generally very close to those with smaller stakes.

6 or below whereas 3 would lose if Buis picked 6 and tie if he picked 5. If go high or low, picking 5 would have been a better choice by Hatch than 7 an expected \$160,000. And, unless one had a reason to think Buis would Buis had picked randomly, by choosing 3 after Hatch's 7 Wigglesworth lost dominated by choosing 6, because 6 would win for any choice by Buis of Hatch chose 7. Astonishingly, Wigglesworth then chose β , a choice that is simply used the contest to create an illusion of fairness, is hard to tell.) to Buis's would win. (Whether Buis actually committed to his number, or to pick integers between I and 9 and the person whose number was closest huge.) The two finalists, Richard Hatch and Kelly Wigglesworth, were asked two others to vote for based on their answers in a simple number game. popular Survivor television show, survivor Greg Buis was deciding which of a very high-stakes situation. In the final round of the first edition of the (Buis claimed he chose 9 and so Hatch won the \$1 million.) (The winner got \$1 million and the runner-up \$100,000, so the stakes are Finally, Rob Kurzban mentioned a great example of poor reasoning in

A1.2.6 Order Effects

Experiments often involve two treatments, A and B. If they are always done in the same order, denoted AB, then any difference in the two treatments might be due to the fact that A came first and B came second (an "order effect"). Order is "confounded with" (perfectly correlated with) the treatment. This is easily controlled by running some sessions in the reverse order, BA, and including an order dummy variable in statistical analyses.

A1.2.7 Controlling Risk Tastes

Even though subjects should be risk-neutral toward small lab gambles (Rabin, 2000), it would be useful to have a procedure for creating payoffs that subjects are risk-neutral towards (i.e., so they are indifferent to the dispersubjects are

sion of possible payoffs around a fixed mean). There is such a procedure—the binary lottery procedure.

In the binary lottery procedure, subjects are paid in lottery tickets, which are later used to determine their chance of winning a lottery for a fixed prize (see Roth and Malouf, 1979). If players reduce compound lotteries to single-stage lotteries, they should be neutral toward mean-preserving spreads in their ticket distribution—that is, they should have linear utility over tickets. For example, if they regard a 0.32 chance of winning fifty tickets (and otherwise getting none) as the same as having sixteen tickets, they are risk-neutral toward tickets. (In theory, the procedure can be extended to induce any shape of utility function by transforming payoff units to tickets nonlinearly; see Schotter and Braunstein, 1981, and Berg et al., 1986.)

Unfortunately, there is little evidence that the binary lottery procedure works as it should in theory (and a couple of studies showing it does not work). For example, in direct tests, players who make choices with monetary payoffs and players who make choices with lottery ticket payoffs exhibit the same patterns, so the binary lottery procedure does not change apparent risk-aversion over money into risk-neutrality over tickets (Camerer and Ho, 1994; Selten, Sadrieh, and Abbink, 1999). On the other hand, Van Huyck and Battalio (1999) found that players behaved consistently with risk-neutrality over tickets (though see their footnote 9 for an opposite result). In the most careful study, Prasnikar (1999) found that risk-aversion coefficients estimated from choices among gambles over tickets were close to of subjects who obeyed reduction of compound lotteries.

It is surprising that many experimenters use the binary lottery procedure despite so little careful evaluation of when it does induce risk-neutrality (and given the evidence that it often doesn't). To paraphrase G. B. Shaw's wisecrack about marriage, faith in the procedure seems to be a triumph of hope over data. There are two alternatives to trying to induce risk tastes: assume risk-neutrality, or measure risk tastes over money independently and use those measures to calibrate an individual subject's risk preferences in a game (which several experimenters have done). In any case, it would be good to see more careful research (à la Prasnikar, 1999) establishing when the procedure works and when it does not.

A1.2.8 Within-Subjects and Between-Subjects Design

In a "within-subjects" design, a single subject is observed in different treatments. (The subject serves as "her own control group".) In a "between-subjects" design—the norm in experimental economics—different subjects are tested in treatments A and B. Statistical variation across the subjects

then muddies the waters of what is observed by comparing A and B. Withinsubject designs are more statistically powerful than between-subject designs because they automatically control for individual differences, which are often a large source of variation, and hence allow the effect of a treatment to shine through when the nuisance of individual difference is controlled for.

There is a curious bias against within-subjects designs in experimental economics (not so in experimental psychology). I don't know why there is a bias, and I can't think of a compelling reason always to eschew such designs. One possible reason is that exposing subjects to multiple conditions heightens their sensitivity to the differences in conditions. This hypothesis can be tested, however, by comparing results from within- and betweensubjects designs, which is rarely done.

A1.2.9 Experimetrics

"Experimetrics" are econometric techniques customized to experimental applications. Although I'm an amateur econometrician, I am a huge fan of experimetrics. The next generation of experimenters should feel obliged to use the very latest inferential tools—the best microscopes—to see patterns in data as clearly as possible. The work by Crawford, El-Gamal, McKelvey and Palfrey, Stahl, and Van Huyck and Battalio described in this book sets a high standard other experimenters should emulate.

A new tool in experimetrics which has not become widely adopted is optimal endogeneous experimental design (e.g., El-Gamal, McKelvey, and Palfrey, 1993). In many experiments, the experimenter has one or more hypotheses that she can put prior probabilities on. A crisp prior, and specification of the hypotheses, can be used to compute the information value (in the sense of dispersion of posterior probabilities relative to dispersion of priors) of different experimental design parameters. This motivates the choice of "optimally informative" design parameters. Furthermore, because of increases in computing power, for the first time in human history we can alter the experimental design in real time—while subjects are waiting, for seconds rather than days—to optimize the amount of information collected in an experiment. (Seen this way, all previous experimental designs are heuristic approximations to endogeneously optimized designs.) Information-optimized designs have rarely been used. The younger generation should embarass us older folks by taking them up with a vengeance.

Dictator, Ultimatum, and Trust Games

on distribution they are to be

IN 1982, GÜTH, SCHMITTBERGER, AND SCHWARZE reported the kind of empirical finding that surprises only economists. They studied an "ultimatum" game in which one player, the "Proposer," makes a take-it-or-leave-it offer, dividing some amount of money between herself and another person. If the second person, the "Responder," accepts the division, then both people earn the specified amounts. If the Responder rejects it, they both get nothing. The ultimatum game could hardly be simpler. If Responders maximize their own money payoffs, they should accept any offer. If Proposers also maximize and expect Responders to maximize, they should offer the smallest amount.

In experiments, Proposers offer an average of 40 percent of the money (many offer half) and Responders reject small offers of 20 percent or so half the time. The data falsify the assumption that players maximize their own payoffs as clearly as experimental data can. Every methodological explanation you can think of (such as low stakes) has been carefully tested and cannot fully explain the results.

Since the equilibria are so simple to compute (the Responder's move is just a choice of a payoff allocation), the ultimatum game is a crisp way to measure social preferences rather than a deep test of strategic thinking (see Marwell and Schnitt, 1968). Measuring social preferences in money terms is important because concepts such as fairness and trust figure prominently in private negotiation and public policy. But many cynics (especially economists) think fairness is simply a rhetorical term used by people who deserve the short end of the stick for trying to get more, and that people will not sacrifice much to punish unfairness or reward fairness. As George