# **Bargaining Outcomes as the Result of Coordinated Expectations**

# AN EXPERIMENTAL STUDY OF SEQUENTIAL BARGAINING

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Experimental studies of two-person sequential bargaining demonstrate that the concept of subgame perfection is not a reliable predictor of actual behavior. Alternative explanations argue that fairness influences outcomes and that bargainer expectations matter and are likely not to be coordinated at the outset. This study examines the process by which bargainers in dyads coordinate their expectations on a bargaining convention and how this convention is supported by the seemingly empty threat of rejecting positive but small subgame perfect offers. To organize the data from this experiment, a Markov model of adaptive expectations and bounded rationality is developed. The model predicts actual behavior quite closely.

**Keywords:** sequential bargaining; experiment; convention; fairness; finite Markov chain; bounded rationality; learning

If the phenomenon of "rational agreement" is fundamentally psychic—convergence of expectations—there is no presumption that mathematical game theory is essential to the process of reaching agreement, hence no basis for presuming that mathematics is a main source of inspiration in the convergence process.

-Schelling (1960, 114)

Experimental studies of two-person sequential bargaining have documented two behavioral regularities—subjects do not end up in subgame perfection equilibria (SGPE), even with experience, and observed outcomes typically diverge from the SGPE toward an equal split of the surplus. Deviations toward equitable outcomes have been examined extensively, and a growing consensus explains this behavior in terms of "social preferences" or, specifically, preferences for fair outcomes (Fehr and

1. For a review of the ultimatum game, see Camerer and Thaler (1995). For sequential bargaining studies, see Gueth and Tietz (1988); Neelin, Sonnenschein, and Spiegel (1988); or Ochs and Roth (1989).

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Schmidt 1999, Bolton and Ockenfels 1999, Rabin and Charness forthcoming). We take as given that narrow self-interest explains only a minority of the behavior seen in the experimental lab (e.g., some market experiments). Instead of focusing on explaining behavior in terms of fairness preferences, we concentrate on the origins of preferences for fairness and make the case that fairness norms may arise in the interaction between social heuristics, institutional settings, and the expectations held by economic agents.

Concentrating for now on the fact that the SGPE does not predict behavior, it is clear that subgame perfection can only be supported if bargainers use SGPE strategies and expect that their opponents will also. In this sense, subgame perfection requires common knowledge of the ability to do backward induction. Experiments have been conducted that indirectly test if subgame perfection is behaviorally important by analyzing whether subjects make backward induction calculations to inform decisions. These studies find little support for a general capacity to do multiple levels of backward induction or iterative dominance.<sup>2</sup> As such, it is unlikely that the key to understanding how subjects reason in sequential bargaining lies in the mechanics of backward induction.

On the other hand, expectations have proven effective in explaining behavior.<sup>3</sup> Experiments that analyze expectations demonstrate that two agents will be able to maintain an efficient (conflict minimizing) outcome only when they come to anticipate the response of their partner. In situations, such as in the experimental lab, that are devoid of the kind of social history that establishes prevailing behavioral conventions, subjects are likely to initially rely on social heuristics. Social heuristics are general behavioral rules developed outside the lab, which, presumably, are shared by all participants from a common culture (Roth et al. 1991; Henrich 2000; and Henrich et al. 2001). In this way, subjects rely on heuristic rules as a benchmark from which they explore alternative strategies within the setting of the experiment. The exploration process consists mainly of forming expectations about the future success of various strategies based on what has worked previously in the current population of bargaining partners. Put another way, bargaining conventions, and adaptive social norms in general, are important, not necessarily because they dictate behavior, but because they coordinate agents' expectations.

The study reports on a repeated sequential bargaining experiment that supports this theory of bargaining conventions. A brief summary of the results follows. To begin, subgame perfection is not supported as a predictor of outcomes. Rather, a convention develops in the early stages of bargaining (despite various treatment conditions that alter the strategic incentives of the game) wherein the bargainer making a proposal gets

<sup>2.</sup> For experimental studies of backward induction, see McKelvey and Palfrey (1992). See Nagel (1995) and Ho, Camerer, and Weigelt (1998) on iterative dominance. For an experiment using the novel approach of monitoring player's search patterns, see Johnson et al. (forthcoming).

<sup>3.</sup> Roth and Schoumaker (1983) demonstrate the importance of expectations in determining bargaining outcomes in an experiment using a two-stage version of the Nash demand game. Additionally, Harrison and McCabe (1996) demonstrate that with exposure to subgame perfect play, subjects eventually coordinate on the subgame perfection equilibria (SGPE). For other experimental studies where expectations are found to be important, see Ochs (1995) on coordination problems and Sunder (1995) on speculative asset market bubbles.

55 percent of the current pie. This convention is supported by the theoretically incredible threat to reject subgame perfect offers. Furthermore, a model of adaptive expectations does well to explain the evolution of this convention, given the starting distribution of bargaining strategies.

## THE EXPERIMENTAL DESIGN

The experiment described below is essentially a simplification of the design used by Harrison and McCabe (1992). The Harrison and McCabe design gives subjects repeated experience in both a three-stage sequential bargaining game and the two-stage subgame of the larger game. This design is used to show that experience in the subgame is enough to coordinate the expectations of subjects in a way that mimics the notion of common knowledge mentioned above. Given this design, the authors find support for subgame perfection as the limiting outcome when subjects gain sufficient experience and, therefore, have coordinated their expectations.

The current experiment exploits the elements of the Harrison and McCabe (1992) design that are useful for examining expectations (i.e., repeated experience in the subgame) but takes cues from experiments that have been run that demonstrate that experimenters should not expect subjects to accomplish more than two levels of backward induction (see Note 2). To account for this stylized fact, the current experiment is a simplified (one- and two-round) version of the earlier study to ensure that subgame perfection is given a fair chance of working. Figure 1 summarizes the repeated sequential bargaining environment that participants faced.

Participants were randomly assigned to roles as player 1 or player 2. There were 15 periods of bargaining. All the odd periods were one-round ultimatum games, and all the even periods were two-round games. In periods 1, 3, . . . 15 player 2 proposed a division, X, of a pie of size  $10\delta$  where  $0 < \delta < 1$  (in the experiment,  $\delta = .25$  or .75). Next, player 1 decided to either accept or reject this proposal. If the proposal was accepted, player 1 received X, and player 2 received  $10\delta - X$ . If the proposal was rejected, both players received 0 for the period.

In periods  $2, 4 \dots 14$ , player 1 made an opening offer over a pie that was initially 10 experimental francs. If player 2 accepted player 1's proposal, the period was over, player 2 received X, and 10 - X went to player 1. However, if player 2 rejected player 1's round-1 proposal, then the two participants moved to round 2—the subgame, and the pie shrank to  $10\delta$ . By design, the resulting subgame was identical to the ultimatum game played in odd periods.

All participants were given a worksheet to ensure that they understood the structure of bargaining. The worksheet required participants to keep a record of proposals sent and received and responses made for each period. As a result, the worksheet clearly laid out the structure of bargaining and therefore reinforced the consequences of moving to the subgame. Also, by filling out the worksheet, each participant had a complete history of prior proposals and responses. This was done to facilitate strategic thinking and give subgame perfection its best shot.

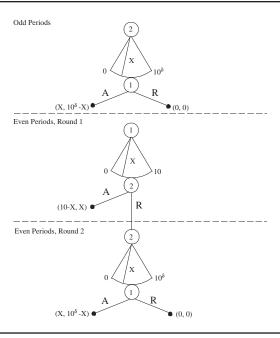


Figure 1: The Bargaining Institution

NOTE: X is the offer,  $0 < \delta < 1$ , A means accept, and R means reject.

The subgame perfect equilibrium for each period is calculated with the help of Figure 1. Start with the subgame played in each odd period. In addition, assume that bargainers have standard preferences for monetary outcomes and common expectations that everyone else has similar preferences; then the SGPE outcome occurs where player 2 offers player 1 the smallest unit of account,  $\epsilon$ , and player 1 accepts because  $\epsilon$  is better than nothing. This is true for each odd period and, thus, forms the expectation of what is likely to occur if bargaining in even periods moves to the subgame. Given this expectation about subgame play, in even periods, player 1 will offer player 2 what player 2 expects to receive if bargaining moves to the second round, namely,  $10\delta$ . Faced with this offer, player 2 accepts because she or he cannot possibly do better by rejecting and forcing the interaction to round 2. This pattern will repeat itself regardless of how participants are matched.<sup>4</sup>

This bargaining environment was chosen for two reasons. First, repeated bargaining is used because it provides the kind of experience that might lead participants to eventually experiment in the direction of the SGPE. Second, this institution forces participants, who otherwise would tend to settle in round 1 of the two-stage game, through

4. Notice that even repeated bargaining between players matched with the same partner for the duration of the game cannot support any other Nash equilibrium. For example, an early rejection by either player 1 or 2 can only sustain a more favorable series of future proposals if the other player is uncertain about the preferences of the rejector. The assumption of common knowledge guarantees that any rejection is treated as a mistake, and therefore the SGPE prediction is also robust with respect to "trembling hands." In addition, the game is finitely repeated, which precludes any folk theorem results.

TABLE 1 Experimental Design

	Matching	Rule		
Discount Factor	Same Pairing	Random Re-Pairing		
$\delta = .25$	Sessions 6,8,9	Sessions 3,5,13		
	15 pairs - 15 periods	11 pairs - 15 periods		
	12 pairs - 10 periods	16 pairs - 10 periods		
$\delta = .75$	Sessions 7, 10, 11	Sessions 2, 4, 12		
	17 pairs - 15 periods	16 pairs - 15 periods		
	17 pairs - 10 periods	15 pairs - 10 periods		

the subgame. The reasoning behind this follows Harrison and McCabe (1992), who posit that pairs of subjects who agree in the first round of a sequential game do not necessarily have common expectations about acceptable outcomes because they lack experience in the subgame. Without subgame experience, these subjects have no way of forming expectations about what they will get in the second round.

Within the experiment, two treatment variables were manipulated: the degree to which the pie shrank in the bargaining game,  $\delta$ , and the rule that matched bargainers at the beginning of each period. Table 1 summarizes the design. For half of the sessions, the discount factor was .25 favoring player 1, and for the other half the discount factor was .75 favoring player 2.5 For half the sessions, participants were matched with the same partner for all 15 periods, and for the other half, participants were randomly rematched at the beginning of each period. The matching rule was explicitly mentioned in the instructions (see the appendix).

#### EXPERIMENTAL RESULTS

A total of 12 sessions were run using undergraduate participants at the University of Massachusetts. The entire experiment (from instructions to payment) lasted slightly less than an hour, and the average earnings of a participant, including \$5.00 for showing up, were \$14.43. To increase the number of pairs in each cell, the current results were pooled with those of a series of experiments run at the University of Arizona. There are two main differences in the experiments. The Arizona experiments were preceded by a preference revelation mechanism and were run for only 10 periods. However, t tests of mean behavior and Kolmogorov-Smirnov tests of distributional differences did not suggest that behavior was significantly different between experiments. After pooling the data, there are  $27 (\delta = .25, \text{same})$  pairs,  $27 (\delta = .25, \text{random})$  pairs, 34

<sup>5.</sup> Remember, player 2 is expected to receive the lion's share of the subgame (ultimatum game) pie. Hence, as  $\delta$  increases, player 2 is the expected beneficiary.

<sup>6.</sup> The preference revelation mechanism was essentially a series of bilateral dictator allocation decisions with variable pie sizes. Participants did not know the outcome of the preference exercise until the end of the experiment. For a more in-depth analysis of the Arizona experiments, see Carpenter (forthcoming).

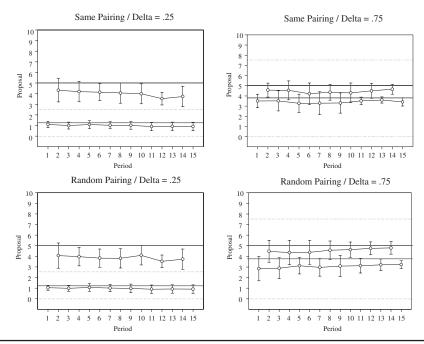


Figure 2: The Average First-Round and Ultimatum Offers by Period (Plus or Minus One Deviation)

NOTE: ° indicates mean proposal,  $\top$  and  $\bot$  are error bars, solid horizontal lines indicate equal splits, and dotted lines indicate the subgame perfect equilibrium.

 $(\delta = .75, \text{same})$  pairs, and 31  $(\delta = .75, \text{random})$  pairs for each of the first 10 periods, and the numbers listed in Table 1 for periods 11 through 15.

The most striking feature of the data is how stationary proposals are over time in both the ultimatum games and the two-stage games. Standard *t* tests indicate that mean first-period proposals are not significantly different from last period proposals for any of the eight sequences. To illustrate this point, Figure 2 plots the amount offered in the first round of the two-stage game played in even periods and proposals made in the ultimatum game played in odd periods and for each cell of the design. Open circles indicate average offers, and the lines above and below indicate plus and minus one standard deviation. Furthermore, solid horizontal lines indicate an even split of the surplus, and dashed lines mark the SGPE predictions. 8

Clearly, these results are at odds with Harrison and McCabe (1992). Whereas Harrison and McCabe find that proposals steadily converge toward the subgame perfect prediction over the course of 14 periods, our results, using a much simpler version of the game, show no movement in that direction. Two differences in the experiments may

<sup>7.</sup> All tests were two-tailed, and no differences were found at the 5% level.

<sup>8.</sup> For all ultimatum games, the SGPE is zero, for  $\delta$  = .25, the first-round prediction is 2.50, and for  $\delta$  = .75, the prediction is 7.50.

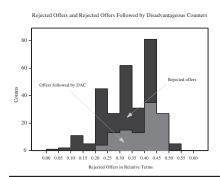
account for this difference. First, in the more complicated Harrison and McCabe game, the theoretical prediction in the two-stage subgame overlapped with an equal split of the surplus. This feature of the design might have made the theorized subgame result more salient in the minds of the participants compared with the very unequal theoretical outcome in the subgame of the current experiment. (Recall the subgame of the current experiment is an ultimatum game.) If this was true, then it may have been easier for the majority of participants to form a common expectation about what would occur in the subgame. However, this explanation is somewhat unsatisfactory because it is reasonable to think that participants who rely on fairness to coordinate expectations in the two-round subgame would also do so when making offers in the three-round game. An alternative explanation might have something to do with the worksheet that participants filled out during the current experiment. Instead of eliciting strategic behavior by stressing the structure of play and the consequences of rejecting an initial offer, the worksheet might have reinforced fair play, because participants often looked at a history of fair offers when recording their responses.

Although the current results differ from those of Harrison and McCabe (1992), it would be a mistake to conclude that expectations do not matter. Instead, the difference in these two experiments only questions whether strict fairness norms (i.e., the equal split) can easily be displaced by experience. As I will show below, expectations might also account for the current results. In the next section, I build a model to argue that proposers quickly formed expectations that were maintained over the course of the experiment and that these expectations did not drive proposals to the levels predicted by subgame perfection; nor did they reflect strict fairness. Instead, these hybrid offers hover just below the equal split reflecting a slight advantage for the proposer. This result is true for both the one-stage ultimatum games and the two-stage shrinking pie games.

It appears that proposers are somewhat affected by the discount factor in the two-stage game. Returning to Figure 2, when  $\delta$  is .25 and player 1 (the initial proposer) has the advantage, first-round proposals are slightly less than when  $\delta$  is .75 and player 2 has the advantage. This supports the hypothesis developed in Gueth and Tietz (1990) that players hide behind fairness and do not offer more than half when the discount factor does not benefit them. I will return to this below when the treatment effects are analyzed more fully. Overall, however, Figure 2 demonstrates that the results can be summarized by a convention wherein the bargainer who is currently proposing gets 55% of the pie and the responder gets the remainder.

Ochs and Roth (1989) coin the term *disadvantageous counterproposals* (*DACs*) for second-round proposals that leave the proposer with less than he or she would have gotten if he or she had accepted the first-round offer. They assert that this is an important phenomenon because it describes 81% of the rejections found in their study and is also not predicted by subgame perfection. The results of the current experiments reveal a substantial amount of DACs (36%), although not as many as in the Ochs and Roth

<sup>9.</sup> One-tailed t tests reject the hypothesis that any sequence approached subgame perfection. 10. In all but two instances ( $\delta$  = .25, same—ultimatum) and  $\delta$  = .25, random—ultimatum), one-tailed t tests demonstrate that offers, pooled across periods, are significantly below the equal split even though in many instances the equal split is continuously within one standard deviation of the mean.



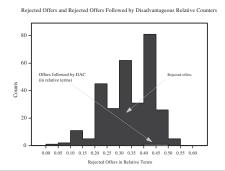


Figure 3: Rejected Offers and Disadvantageous Counterproposals (DACs)

NOTE: The dark histograms represent all the offers, the light histogram on the left represents offers that were rejected and then followed by a DAC in absolute terms, and the light histogram on the right represents rejected offers followed by DACs in relative terms.

study. <sup>11</sup> Rejected offers, in relative terms so that the data could be pooled across different values of  $\delta$ , and DACs that followed rejected offers, are illustrated in the left panel of Figure 3.

Figure 3 should be read as follows. The darker region in both panels is a histogram of offers (in relative terms) that were rejected. The lighter region in the left panel is a histogram of relative offers that were rejected and followed by DACs. This panel illustrates the fact that a significant number of relatively fair offers are rejected and followed by DACs. The lighter region in the right panel is a histogram of DACs, but in relative terms (i.e., counterproposals that gave player 2 less in relative terms than the first-round proposal that was rejected). Bolton (1991) explains DACs by arguing that subjects value both absolute and relative outcomes. That is, a subject may reject a round-1 proposal and counter by asking for less in absolute terms; however, the resulting counterproposal may give the proposer a larger share of the smaller pie. This explanation is supported by the right panel of Figure 3. Here, the small, lighter histogram illustrates that only 2 of the 105 DACs are disadvantageous in relative terms. That is, in 98% of the cases, participants rejected offers and countered by asking for more in relative terms.

An analysis of the actual counterproposals suggests two mechanisms that support the evolution of the 55/45 convention. As just mentioned, bargainers reject offers that are small in relative terms and counter with proposals that ask for a larger relative share. However, how much more (in relative terms) do they ask for? Basically, there are two types of counterproposals. In the first case, player 2 rejects a low first-round offer and counters by returning to the 55/45 convention (i.e., asks for 55% of the second-round pie). The second type escalates the aggressive offer of player 1 by rejecting and

<sup>11.</sup> The reason that the amount of disadvantageous counterproposals (DACs) is lower in the current study is probably because of the discount factors used. Virtually all counterproposals in the  $\delta$  = .25 sessions are disadvantageous. However, many of the  $\delta$  = .75 counterproposals are not disadvantageous because by rejecting a low offer in round 1, a player can still receive a substantial amount in round 2. By comparison, Ochs and Roth (1989) used  $\delta$ s of .4 and .6.

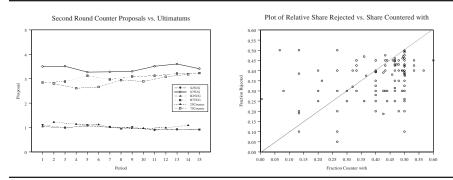


Figure 4: Second-Round Counterproposals

NOTE: Each circle in the right panel represents a rejected offer and the counteroffer that followed in relative terms.

responding with an even lower counteroffer. This second type is a sort of tit-for-tat player who punishes departures from the convention by escalating the deviation. The first type simply returns to the convention when deviations are encountered.<sup>12</sup>

The size of the second-round pie influences the distribution of these two types of counterproposers in the population. When the pie shrinks a lot between round 1 and round 2 ( $\delta$  = .25), many more player 2s respond to low proposals by returning to the norm. However, when the pie does not shrink much ( $\delta$  = .75), more player 2s escalate the deviation from the norm. The treatment effect of  $\delta$  on counterproposals is demonstrated in the left panel of Figure 4. In Figures 4 and 5, the first letter in the abbreviation stands for the matching rule, same or random, the number corresponds to the discount factor, the abbreviation SR represents the first-round offer of the Ståhl-Rubinstein game played in all even periods, and UG is obvious. In the  $\delta$  = .25 case, one can see that counterproposals are indistinguishable from odd period ultimatum offers. <sup>13</sup> However, when  $\delta$  = .75, counterproposals are on average less than their odd period counterparts, which suggests the escalation of low offers in this case. <sup>14</sup>

The heterogeneity in counterproposing behavior is better demonstrated in the scatter plot in the right panel of Figure 4, which plots rejected offers in relative terms against the fraction of the round-2 pie that was counterproposed. Here, one sees a large mass of data below the 45 degree line, perhaps reflecting the inequality aversion of some participants. Also note the mass of observations between the 40% and 50% counterproposal, which illustrates those players who return to the convention. However, one also sees a considerable amount of tit-for-tat play to the northwest of the 45 degree line.

<sup>12.</sup> Note that these results are consistent with many distribution and inequality based models of preferences. Examples include Fehr and Schmidt (1999), Bolton and Ockenfels (1999), and Falk and Fischbacher (1998).

<sup>13.</sup> Counterproposals are not different from the ultimatum offers in the  $\delta$  = .25, same treatment (t = 1.02, p = .15); nor are they different from the  $\delta$  = .25, random treatment (t = 1.41, p = .08).

<sup>14.</sup> Here, counterproposals are marginally different from the  $\delta$  = .75, random treatment (t = -1.76, p = .04) and highly significantly different from the  $\delta$  = .75, same treatment (t = -5.29, p < .01).

<sup>15.</sup> For a general theory of inequality aversion, see Fehr and Schmidt (1999).

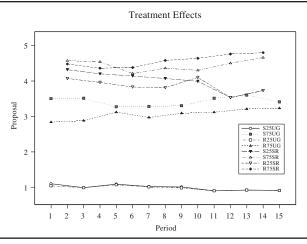


Figure 5: Treatment Effects

NOTE: In the legend, the first letter indicates the player matching protocol—same versus random—the number indicates the value of  $\delta$ , UG means the subgame, and SR means the first offer in the two-round game.

The final thing to notice about counterproposals is that they are more likely to be rejected than first-round proposals (34% of counters are rejected versus 21% of first-round proposals). This observation also suggests that the punishment implicit in a first-round rejection is often escalated. Controlling for offer size, pie size, and the subject-pairing rule, the following random effects logit regression shows that offers are significantly (p < .01) more likely to be accepted in the odd period ultimatum games than in the second round of the even period Ståhl-Rubinstein games.

Response (accept = 1) = 
$$0.75 + 2.01$$
Offer  $-0.78$ Pie  $-0.20$ Pairing  $+1.57$ UG (0.41) (0.25) (0.11) (0.28) (0.32) Wald  $\chi^2 = 77.06$ ,  $p < .01$ .

Turning to a discussion of the treatment effects, one sees that varying the discount factor has a strong effect on behavior, whereas manipulating the matching rule influences behavior to a lesser extent. Figure 5 illustrates the differences between treatments by plotting all eight sequences of average offers by period. One can see the striking difference in first-round behavior between the  $\delta=.25$  and  $\delta=.75$  treatments (compare S25SR to S75SR and R25SR to R75SR).  $^{16}$  Regardless of the pairing rule, the average offers of the  $\delta=.75$  treatment always lie above their  $\delta=.25$  counterparts and continue to separate as the experiment progresses. This phenomenon further supports the idea that proposers push the other player harder when the discount factor favors them but hide behind fairness when they are in the theoretically disadvantaged position.

16. Kolmogorov-Smirnov (KS) tests show that the differences between the distributions of offers for both pairing conditions are significant at any level.

The pairing rule has less effect. There were significant differences in behavior in only two instances. First and surprisingly, first-round offers in the two-round game ( $\delta = .75$ ) were significantly higher when bargainers were randomly repaired after every round than when bargainers stayed with the same partner for the duration of the experiment.<sup>17</sup> Second, and as one would expect if repeat interaction supports sharing, offers in the odd period ultimatum games where  $\delta = .75$  were significantly higher when bargainers were paired with the same partner for the entire experiment than when they were reshuffled after every period.<sup>18</sup> In the other two cases (first-round proposals where  $\delta = .25$ , ultimatum proposals where  $\delta = .25$ ), there was no significant effect of the matching rule.

## COORDINATED EXPECTATIONS AND BARGAINING OUTCOMES

The lack of variation in proposals across treatments with respect to time suggests that participants quickly agreed on a convention that guided proposing behavior. This convention, although obviously linked to fairness, evolved away from the equal split in response to the institutional rules of the experiment. Additionally, it has been shown that the rejection behavior of participants works to support this convention by punishing deviations from the established norm and by returning to it with counterproposals. However, as an explanation of the evolution of the 55/45 convention, it is still conjecture to say that the driving force is coordinated expectations. In this section, I will build and discuss a model of adaptive expectations. The purpose of the model is to illustrate how, given the initial expectations of participants and despite the fact that interaction occurred in dyads, the most likely convention to evolve based on the decentralized flow of information between participants is the one observed—proposers get 55% of the pie.

The structure of the model is adapted from a discussion of the evolution of conventions in Young (1993), Young (1998), and Gintis (2000). More specifically, I will first develop a deterministic model of adaptive expectations in which a pseudo-Markov transition matrix is constructed based on best-reply dynamics applied to initial expectations about the success of three particular proposing strategies. These three strategies organize all of the first proposals made by participants. For what follows, *bargaining conventions* will be defined broadly as the states of the resulting dynamic system that demonstrate the most attracting power. In the initial model, conventions will simply be absorbing states. When I complicate the model later on, conventions in the resulting ergodic system will be the states in which the system spends most of its time.

To begin, I define three proposing strategies. The first will be called Low(L) and will be defined as making a proposal, x, to one's counterpart for less than 40% of the

<sup>17.</sup> KS = .1545, p = .02.

<sup>18.</sup> KS = .2451, p < .01.

<sup>19.</sup> Note, however, that the resulting convention only moves in the direction of the SGPE in the case of the low-discount factor. In the high-discount factor treatments, the SGPE requires the proposer to offer more than half the pie in two-round games. This suggests that instead of responding to the theoretical structure of the game, participants associated bargaining power with the role of proposing.

			Player 2	
		L	H	C
Player	L	0.52, 0.67	0.48, 0.49	0.49, 0.58
1	H	0.42, 0.43	0.51, 0.47	0.48, 0.43
	C	0.50, 0.32	0.52, 0.46	0.51, 0.56

Figure 6: The Expected Payoff to Each Strategy (in Relative Terms)

NOTE: L = low; H = half; C = convention.

pie (i.e.,  $L = \{x | x < .4(current pie)\}$ ). Notice that in the ultimatum game (periods 1, 3 . . . 15) and in even periods when the discount factor is .25, the L proposing strategy includes behavior that would be expected from participants offering the SGPE. Considering first proposals across treatments (i.e., considering only period 1 in the case of player 2s and period 2 in the case of player 1s), the strategy L accounts for 17% of proposals. The second strategy will be called Half(H), which is played by proposing at least half the current pie to one's opponent (i.e.,  $H = \{x | x \ge .5 \text{ (current pie)}\}$ ). In the first two periods, H was played by 49% of player 2s and by 47% of player 1s. Last, define the strategy C as the *bargaining convention* where proposers get approximately 55% of the current pie (i.e.,  $C = \{x | .4 < x < .5 \text{ of the current pie}\}$ ). Strategy C was played by 36% of player 1s and by 35% of player 2s when making their first proposals.

Using these three strategies to organize the data on proposals for the first two periods, one can calculate the average (and expected) payoff of each strategy. I use the data from the first two periods only, because I am interested in how behavior and expectations adapt to the results of initial play. Figure 6 presents the expected payoff to each strategy when it meets a proposer who makes a proposal of either L, H, or C. The entries of Figure 6 are in relative terms. I will continue to speak in terms of relative proposals so that the data from all four cells can be pooled and because the development of the observed convention appears to be independent of the treatment conditions.

Define an *expectational equilibrium* as a Nash equilibrium of the game played between proposers where the payoffs are expressed as expectations. Clearly, for player 1, proposing half is dominated in expected payoff by playing the C strategy. On further examination, one can see that there are two expectational equilibria based on play in the first two periods. Both are symmetric and occur where all proposers coordinate on proposing L or all play C. Referring to the definition of Nash equilibria, it should be clear that the expectational equilibria in Figure 6 will be absorbing states in this model of adaptive expectations. In other words, once bargainers transit to one of the equilibrium states, LL or CC (to be read player 1's strategy, player 2's strategy),

<sup>20.</sup> The payoffs in Figure 6 were calculated as the average payoff in period 1 (period 2) for player 2 (player 1) of the encounters between player 2 who played the low (L), high (H), or contention (C) strategy when matched with a player 1 who subsequently played L, H, or C on the next round and between player 1 who played L, H, or C on the round before.

<sup>21.</sup> Note, however, that such a model would not necessarily predict that the resulting dynamic system would be driven toward the SGPE. Things such as the spite witnessed in the current experiment might prevent such convergence.

		LL	LH	LC	HL	HH	HC	CL	CH	CC
	LL	1	0	0	0	0	0	0	0	0
	LH	0	0	0	0	0	0	1	0	0
	LC	0	0	0	0	0	0	1	0	0
	HL	0	1	0	0	0	0	0	0	0
E =	HH	0	0	0	0	0	0	0	1	0
	HC	0	0	0	0	0	0	0	1	0
	CL	0	0	1	0	0	0	0	0	0
	CH	0	0	0	0	0	0	0	0	1
	CC	0	0	0	0	0	0	0	0	1

Figure 7: Best-Reply Transition Matrix NOTE: L = low; H = half; C = convention.

their expectations will be coordinated in that they have no incentive to play anything else. The question then becomes, at which equilibrium are participants most likely to end up?

The dynamic I will use is best reply based on one period of recall. Hence, the transition matrix will be deterministic and not stochastic, but, as a first step in the analysis, I am interested to see where best-reply dynamics will drive the data. More specifically, I assume players remember only the last proposal they made and its payoff. Therefore, on average, the dynamics of the population of bargainers can be represented by two agents who play their best reply based on the expected payoffs in Figure 6 and their last encounter. For example, because LL is an absorbing state, the best reply for player 1 of ending up in the LL cell is to continue to play L; likewise for player 2. Similarly, the best reply of player 1, whose last period outcome was HH, is to play C; whereas player 2 will stick with H.

I develop a pseudo-Markovian transition matrix for the current model by calculating the probability of transiting from one state to another of the game illustrated in Figure 6. Because I use the simple best-reply dynamic and because none of the expected payoffs that need to be compared are equal, the transition probabilities are either 0 or 1 (i.e., there is always a unique best reply to the stated history). The resulting best-reply transition matrix, *E*, appears as Figure 7.

Given the assumption that expectations adapt according to the best-reply dynamic used to create E, the predicted distribution of states in the second period of the experiment is calculated by multiplying the distribution of starting states,  $S_0$ , by the transition matrix E. Effectively, this calculates the best reply of the starting population distribution to the expected payoffs of each strategy in the game depicted in Figure 6. Likewise, to calculate the expected distribution of states in period 3, one would multiply  $S_0$  by  $E^2$ . In general, to calculate the distribution of states after n periods, I find  $S_0E^n$ .

Because the transition matrix has absorbing states (that conform to the Nash equilibria of Figure 6), the process of expectation adaptation is likely to be absorbed by either *LL* or *CC*. The question of interest is, which state is more likely to become a

		LL	LH	LC	HL	НН	НС	CL	CH	CC
	LL	1	0	0	0	0	0	0	0	0
	LH	0	0	1	0	0	0	0	0	0
	LC	0	0	1	0	0	0	0	0	0
	HL	0	0	0	0	0	0	1	0	0
$E^* =$	HH	0	0	0	0	0	0	0	0	1
	HC	0	0	0	0	0	0	0	0	1
	CL	0	0	0	0	0	0	1	0	0
	CH	0	0	0	0	0	0	0	0	1
	CC	0	0	0	0	0	0	0	0	1

Figure 8: The Long Run

NOTE: L = low; H = half; C = convention.

convention? In other words, what is the long-run behavior of the system? To examine limiting behavior of the model of expectation coordination, I calculate

$$E^* = \lim_{n \to \infty} E^n$$
.

In this case,  $E^* = E^k$ ,  $\forall k \in \mathbb{N}$ . The resulting matrix appears as Figure 8.

As one can see, if the best-reply dynamic that underlies *E* represents the process of expectation coordination, then those pairs that start in state *LL* will remain there, and those that start in states *LH* and *LC* will be absorbed by state *LC* where player 1 plays *C* and player 2 plays *L*. Furthermore, pairs starting in states *HL* and *CL* will be absorbed by *CL*; and finally, pairs starting in states *HH*, *HC*, *CH*, or *CC* will converge on the convention observed in the data.

Returning to the data on proposals from periods 1 and 2 of the experiment, it is found that  $S_0 = .06$ , .06, .05, .06, .27, .13, .06, .12, .19. Multiplying  $S_0$  by the long-run steady state of the expectation adaptation process,  $E^*$ , results in the end state distribution  $S_0 = .06$ , 0, .11, 0, 0, 0, .12, 0, .71. In other words, the model predicts that 71% of participants will be in dyads that play the C strategy. Overall, if the model accurately predicts the process of expectation coordination, 82% of the bargainers will play C, 18% will play L, and no one will play H.

Now, compare the predicted distribution of bargaining strategies to the actual end state of the experiment. In period 14, player 1s were distributed as follows: 16% *L*, 31% *H*, and 53% *C*. In period 15, player 2s were distributed 25% *L*, 25% *H*, and 50% *C*. On average, pooling 1s and 2s, one finds 21% *L*, 28% *H*, and 51% *C*. Therefore, although the model is not a bad predictor, it overpredicts the absorbing power of the convention and underpredicts the attracting power of proposing half (i.e., it underpredicts the resiliency of the expectations of players who subscribe to an equity norm).

To try to understand the difference between the predicted distribution of proposing strategies and the actual distribution, one can explore relaxing the assumptions made about the dynamic that underlies the expectational transition matrix, *E*. In particular, it

		LL	LH	LC	HL	НН	НС	CL	CH	CC
	LL	$(1-e)^2$	0	(1-e)e	0	0	0	e(1-e)	0	$e^2$
	LH	0	0	0	e(1-e)	0	$e^2$	$(1-e)^2$	0	(1-e)e
	LC	e(1-e)	0	$e^2$	0	0	0	$(1-e)^2$	0	(1-e)e
	HL	(1-e)e/2	$(1-e)^2$	(1-e)e/2	0	0	0	$e^{2}/2$	e(1-e)	$e^{2}/2$
$E_e =$	HH	0	0	0	$e^{2}/2$	e(1-e)	$e^{2}/2$	(1-e)e/2	$(1-e)^2$	(1-e)e/2
	HC	$e^{2}/2$	e(1-e)	$e^{2}/2$	(1-e)e/2	0	(1-e)e/2	0	$(1-e)^2$	0
	CL	0	(1-e)e	$(1-e)^2$	0	0	0	e(1-e)	$e^2$	0
	CH	0	0	0	0	$e^2$	e(1-e)	0	(1-e)e	$(1-e)^2$
	CC	0	$e^2$	e(1-e)	0	0	0	0	(1-e)e	$(1-e)^2$

Figure 9: Second-Best Reply Matrix with e Decision Drift NOTE: L = low; H = half; C = convention.

is obviously incorrect to assume that bargainers can make best replies when they do not have the information to calculate the expected payoffs for each cell of Figure 6. Therefore, one can examine another more boundedly rational dynamic. Rather than assuming that agents make best replies to their first proposals, assume that they sometimes make errors because they do not know what the best reply is or they cannot identify it from their limited sample of play. That is, now assume that bargainers are only able to make best replies (1 - e) of the time, and with probability e, bargainers choose their second-best reply. To justify this change, one might imagine that because players meet one responder at a time, they have not been exposed to enough responders to form the payoff expectations inherent in Figure 6. As a result, with imperfect information, they are forced to make boundedly rational strategy choices. For example, return to Figure 6, where the best reply to ending in state HH for player 1 is to play C. Now, if player 1 does not experience playing C against H, then the best reply is to stick with H. Transforming the matrix E by incorporating the probability, e, of playing the secondbest reply results in the Second-Best Reply transition matrix, which appears in Figure 9.

Because there is a positive probability of moving from any state to any other state (not necessarily in one move),  $E_e$  is ergodic, and one can calculate the predicted long-run distribution directly by finding  $E_e$ \* where

$$E_e^* = \lim_{n \to \infty} E_e^n$$
.

The matrix  $E_e^*$  arises after seven iterations and is a  $9 \times 9$  matrix of the same 9 row vectors. The expectational equilibrium of the second-best reply dynamic is described by this row vector. The first thing to note is that  $E_e^*$  converges quickly, as does  $E^*$ . In fact, both matrices, remarkably, converge within the time frame of the experiment (i.e.,  $\leq 15$  time periods). Figure 10 illustrates the equilibrium predicted distribution of states for three levels of e. It is clear from Figure 10 that the frequency of bargainers playing the H strategy increases as e increases, and therefore, as bargainers become more boundedly rational, they are more likely to continue playing H.

As Figure 10 demonstrates, the model fits better as one relaxes the assumption that bargainers play best responses to the expected payoff of the three strategies. When the probability that agents make second-best responses rather than best responses is .5, the model of coordinated expectations fits rather closely to the behavior observed in the

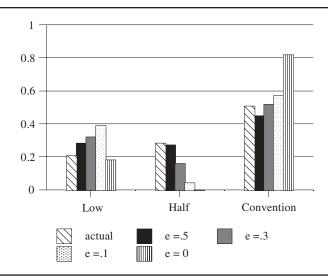


Figure 10: The Predicted versus Actual State Distributions

lab. Summarizing, this suggests that bargaining conventions may arise as an epiphenomenon of the actions of decentralized bargainers who make best responses to available information, given that they may feel some gravity toward preexisting heuristics. Moreover, it is reasonable to think of bargainers as locally optimizing in that they make best-reply comparisons of current payoffs to the outcome of past negotiations. In the process of doing so, a convention arises that is founded on both existing norms (e.g., fairness) and the coordinated expectations that evolve as a by-product of making boundedly rational comparisons within a specific institution.

# DISCUSSION

While the Schelling quote we started this paper with implies that we should not expect bargainers to act like game theorists, this paper illustrates that game theory can help predict the outcome of negotiations. Figure 11 is a nice summary of the data generated by the current experiment. Figure 11 reworks Figure 2 so that the vertical axis now measures relative proposals. Plotting relative proposals in both odd period ultimatum games and even period-2 round games on the same graph clearly illustrates the convention of the proposer (regardless of player number) getting a little more than half. The sequences of proposals plotted in Figure 11 show that regardless of the treatment variables, which have a slight effect on the level of the convention, proposals are flat with respect to time. This regularity and the corresponding reduction of variance in proposals is evidence that expectations have stabilized. That relative proposals overlap so tightly suggests that the convention resulting from coordinated expectations is established in terms of the proposer's share of the given pie rather than in absolute payoffs.

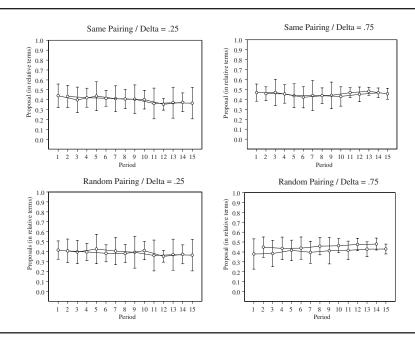


Figure 11: Coordinated Expectations and Relative Proposals NOTE:  $^{\circ}$  indicates mean proposal,  $\top$  and  $\bot$  are error bars.

Although Figure 11 illustrates that proposals have stabilized, for expectations to be truly coordinated one would also anticipate that the rate of rejection would diminish over the course of the experiment. This would occur as participants started to sort out an agreeable allocation for each role. Figure 12 plots the rejection rates for the two roles in the experiment. The first thing to notice is that the rejection rates for the two roles cycle, starting relatively low, increasing, and then falling again. Also notice that the cycles are staggered by one period. After player 1s reject, more (less) player 2s increase (decrease) their likelihood of rejecting in the next period. The path dependant nature of this cycle continues over the course of the experiment, demonstrating that spite might be affecting responses (recall the regression results). If spite is causing the cycles in the responses, it also prevents the rejection rates from systematically diminishing over time. The figure leads to an interesting hypothesis worthy of further study. Namely, if bargainers coordinate their expectations about who should get what in a particular bargaining institution, then one would expect that by the end of a series of negotiations, most offers would be accepted. However, just as general norms of fairness might influence the direction and speed of convergence to a convention within a specific institution, spite might interfere and hinder the process. Here spite, triggered by having one's last offer rejected, disrupts convergence by causing bargainers to reject offers that might have otherwise been acceptable.

Overall, the current results seem to be driven both by distributional concerns and by expectations formed early in the game. As a result, a nonadaptive, norm-driven expla-

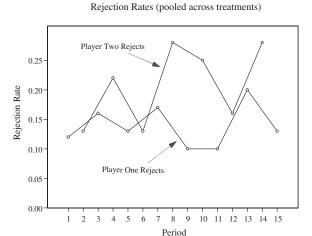


Figure 12: Rejection Rates

nation such as that originally offered in Gueth, Schmittberger, and Schwarz (1982) cannot fully explain these results, because it does not predict the slight but robust deviation from the equal split. At the same time, however, an explanation based solely on eventually attaining common expectations that reflect the strategic incentives built into the game is also unable to explain these results. Such an approach cannot account for the fact that in this experiment, participants never reach the SGPE as they did in Harrison and McCabe (1992). Instead, both explanations seem to be partially true. Hence, a reasonably parsimonious model of the current data would posit agents who enter the experiment with prior expectations that are initially anchored to a distributional norm but adapt to the current institutional arrangement (i.e., the incentives and rules of the game) and the history of play.

As a first attempt at creating such a model, this study has developed a simple model of adaptive expectations that has been calibrated by the expected payoffs faced by bargainers early in the experiment. Overall, the model approximates the behavior seen in the lab in that it predicts expectational equilibria that arise on a time scale similar to the experiment length. However, the fit was drastically improved by weakening the assumptions underlying the best-reply dynamic used. The altered model allows for boundedly rational agents who make best replies to available information. The main contribution of the experiment and the analysis presented here is the evidence to support the idea that more than the underlying logic of strategic interaction, initial conditions and expectations based on the history of play are the driving force behind bargaining outcomes.

Admittedly, the model presented above is a first attempt to create a dynamic explanation of bargaining conventions based on experimental data. The list of interesting extensions and modifications is long. For example, currently, spite only enters the model by affecting the expected payoff of making an offer. Judging by Figure 12, the model might be improved by modeling spite more systematically because the current

model cannot account for the escalation-reduction cycles seen in the data. In another expensive variation of the current methodology, one could abandon the best-reply dynamics we have used to motivate the adaptation process and run enough sessions to create a stochastic transition matrix. Here, the matrix would be based on estimates of actually transiting from one state to another. Finally, one might also consider reworking the types of errors that have been used to create drift in the model. Currently, agents are assumed to lack enough information to always find their best response. Another reasonable approach would be to model errors that cause deviations both for informational reasons and for preference reasons. This might incorporate the models of non-standard preferences developed in Fehr and Schmidt (1999), Bolton and Ockenfels (1999), Falk and Fischbacher (1998), or Rabin and Charness (forthcoming).

# APPENDIX Instructions for Participants (Random Matching Treatment)

This experiment is about two-person bargaining. The experiment consists of 15 periods of bargaining between you and another player in the room. All participants are currently reading the same instructions. At the beginning of each period, you will be randomly matched with another player, and therefore, the likelihood of you being paired with the same player twice is small. You and the person with whom you are matched will bargain over how to split a sum of experimental francs (F) called the "pie." The exchange rate between F and dollars is 1F equals 20 cents.

Each period consists of either 1 or 2 rounds. All odd periods contain only 1 round, and all even periods contain 2 rounds. A round consists of one party's making an offer and the other party accepting or rejecting it. Therefore, in odd periods (1, 3, 5, 7, 9, 11, 13, 15), one party will make an offer, and the other party will decide to accept or reject the offer. If the offer is accepted, your final payoff and the final payoff of the other player will increase by the negotiated split of the pie. If the offer is rejected, then both you and the other player will receive 0F for this round. Once the second party makes this decision, we will wait until all other pairs of subjects have made their choices and then move on to the next period.

All even periods (2, 4, 6, 8, 10, 12, 14) consist of 2 rounds. In the first round, one player will make an offer, and the other will decide to accept or reject the offer. If this player accepts the offer, you will move on to the next period. If this player rejects the offer, the second player will have the opportunity to make a counterproposal in the second round. In the second round, the player who has just rejected an offer will make a counterproposal, and the player who made the original offer will be faced with the decision to accept or reject the counterproposal. Additionally, in the second round the size of the pie will shrink. Therefore, if bargaining in even periods moves to the second round, then both parties incur a penalty. Once both players have made their choices in the second round, we will wait for all the other participants and then move to the next period.

When bargaining begins, the half of the screen to the right of these instructions will be filled with buttons, message boxes, and information. The message box at the top of the screen will inform you whether you are to make an offer or wait for an offer. Also, this box will tell you the status of the offer you have sent to the person with whom you are paired. Below this box are two boxes telling you what period and round it is. Below these boxes is a frame that appears in yellow that displays the offer that is being proposed to you. You will see both how much you will get and

how much the other player will get if you accept the offer. You will notice that the sum of what you get and what the other player gets always equals the current pie size.

The current pie size is always displayed below the offer frame. In addition to the current size of the pie, you will see information about the size of the pie in the previous round and next round (if there is a next round).

If the period is odd (1, 3, 5, 7, 9, 11, 13, 15), then only this period's pie will be displayed because there is only one round in odd periods. If the current period is even (2, 4, 6, 8, 10, 13, 14) and it is round 1, then you will see the size of the pie this round and the size of the pie next round after accounting for the penalty. If the period is even and it is round 2, then you will see the current value of the pie and the value of the pie last round. When it is your turn to make a proposal to the other player, you will see a MAKE PROPOSAL button, another message box, and a SEND PROPOSAL button. The message box at the top of the screen will prompt you to make a proposal. To make a proposal, click on the MAKE PROPOSAL button. An input box appears asking you how much you would like to propose that the other player gets. You will enter an amount between 0 and the current pie size. This is the amount that the other player will receive.

When you click OK, a message appears in the textbox to the right of the MAKE PROPOSAL button that states the terms of the proposal your are offering. If this is what you want to propose, then send it to your partner by clicking SEND PROPOSAL. If you want to readjust your proposal, click the MAKE PROPOSAL button again. If you are in the position to receive an offer in the current round, then you will be told to wait for the other player to send a proposal. When the proposal arrives, it will be displayed in the yellow frame, and the buttons to ACCEPT PROPOSAL or REJECT PROPOSAL will be activated. The text boxes next to these two buttons tell you the consequences of accepting or rejecting an offer. When the current period is even and it is round 1, if you reject a proposal then you will have the opportunity to make a counterproposal over the pie displayed as "Value of Pie NEXT ROUND." If you accept any offer, you will move to the next period.

Your total payoff for the experiment will be the sum of all the Fs that you negotiate in the 15 periods. You have been provided with a worksheet to keep track of your earnings for this segment. Please fill out the worksheet as bargaining proceeds. If you have any questions, please raise your hand now. Otherwise, click the FINISHED button to let us know that you have completed reading the instructions. Once bargaining has begun, it is vital that you make your decisions silently. A summary of the instructions will always appear in this textbox once we have begun the bargaining.

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